Nicholas J. Horton Randall Pruim Daniel T. Kaplan

A Student's Guide to



Project MOSAIC

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Edition 1.3, June 2018

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Cover Photo: Maya Hanna.

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About These Notes

We present an approach to teaching introductory and intermediate statistics courses that is tightly coupled with computing generally and with R and RStudio in particular. These activities and examples are intended to highlight a modern approach to statistical education that focuses on modeling, resampling based inference, and multivariate graphical techniques. A secondary goal is to facilitate computing with data through use of small simulation studies and appropriate statistical analysis workflow. This follows the philosophy outlined by Nolan and Temple Lang¹. The importance of modern computation in statistics education is a principal component of the recently adopted American Statistical Association's curriculum guidelines².

Throughout this book (and its companion volumes), we introduce multiple activities, some appropriate for an introductory course, others suitable for higher levels, that demonstrate key concepts in statistics and modeling while also supporting the core material of more traditional courses.

A Work in Progress

These materials were developed for a workshop entitled *Teaching Statistics Using R* prior to the 2011 United States Conference on Teaching Statistics and revised for US-COTS 2011, USCOTS 2013, eCOTS 2014, ICOTS 9, and USCOTS 2015. We organized these workshops to help instructors integrate R (as well as some related technologies) into statistics courses at all levels. We received great feedback and many wonderful ideas from the participants and those that we've shared this with since the workshops.

¹ D. Nolan and D. Temple Lang. Computing in the statistics curriculum. *The American Statistician*, 64(2):97–107, 2010

² ASA Undergraduate Guidelines Workgroup. 2014 curriculum guidelines for undergraduate programs in statistical science. Technical report, American Statistical Association, November 2014. http: //www.amstat.org/education/ curriculumguidelines.cfm

CAUTION!

Despite our best efforts, you WILL find bugs both in this document and in our code. Please let us know when you encounter them so we can call in the exterminators. Consider these notes to be a work in progress. We appreciate any feedback you are willing to share as we continue to work on these materials and the accompanying mosaic package. Drop us an email at pis@mosaic-web. org with any comments, suggestions, corrections, etc.

Updated versions will be posted at http://mosaic-web. org.

Two Audiences

We initially developed these materials for instructors of statistics at the college or university level. Another audience is the students these instructors teach. Some of the sections, examples, and exercises are written with one or the other of these audiences more clearly at the forefront. This means that

- 1. Some of the materials can be used essentially as is with students.
- 2. Some of the materials aim to equip instructors to develop their own expertise in R and RStudio to develop their own teaching materials.

Although the distinction can get blurry, and what works "as is" in one setting may not work "as is" in another, we'll try to indicate which parts fit into each category as we go along.

R, RStudio and R Packages

R can be obtained from http://cran.r-project.org/. Download and installation are quite straightforward for Mac, PC, or linux machines.

RStudio is an integrated development environment (IDE) that facilitates use of R for both novice and expert users. We have adopted it as our standard teaching environment because it dramatically simplifies the use of R for instructors and for students. RStudio can be installed as a desktop (laptop) application or as a server application that is accessible to users via the Internet.

In addition to R and RStudio, we will make use of several packages that need to be installed and loaded separately. The mosaic package (and its dependencies) will MORE INFO Several things we use that can be done only in RStudio, for instance manipulate() or RStudio's integrated support for reproducible research).

RStudio server version works well with starting students. All they need is a web browser, avoiding any potential problems with oddities of students' individual computers. be used throughout. Other packages appear from time to time as well.

Marginal Notes

Marginal notes appear here and there. Sometimes these are side comments that we wanted to say, but we didn't want to interrupt the flow to mention them in the main text. Others provide teaching tips or caution about traps, pitfalls and gotchas.

What's Ours Is Yours – To a Point

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Document Creation

This document was created on June 29, 2018, using

- knitr, version 1.20
- mosaic, version 1.2.0
- mosaicData, version 1.2.0
- R version 3.5.0 (2018-04-23)

Inevitably, each of these will be updated from time to time. If you find that things look different on your computer, make sure that your version of R and your packages are up to date and check for a newer version of this document.

Kudos to Joseph Cappelleri for many useful comments on earlier drafts of these materials and to Margaret Chien for her work updating the examples to ggformula. Have a great suggestion for a marginal note? Pass it along.

DIGGING DEEPER If you know LATEX as well as R, then knitr provides a nice solution for mixing the two. We used this system to produce this book. We also use it for our own research and to introduce upper level students to reproducible analysis methods. For beginners, we introduce knitr with RMarkdown, which produces PDF, HTML, or Word files using a simpler syntax.

Project MOSAIC

This book is a product of Project MOSAIC, a community of educators working to develop new ways to introduce mathematics, statistics, computation, and modeling to students in colleges and universities.

The goal of the MOSAIC project is to help share ideas and resources to improve teaching, and to develop a curricular and assessment infrastructure to support the dissemination and evaluation of these approaches. Our goal is to provide a broader approach to quantitative studies that provides better support for work in science and technology. The project highlights and integrates diverse aspects of quantitative work that students in science, technology, and engineering will need in their professional lives, but which are today usually taught in isolation, if at all.

In particular, we focus on:

- *Modeling* The ability to create, manipulate and investigate useful and informative mathematical representations of a real-world situations.
- *Statistics* The analysis of variability that draws on our ability to quantify uncertainty and to draw logical inferences from observations and experiment.
- *Computation* The capacity to think algorithmically, to manage data on large scales, to visualize and interact with models, and to automate tasks for efficiency, accuracy, and reproducibility.
- *Calculus* The traditional mathematical entry point for college and university students and a subject that still has the potential to provide important insights to today's students.

Drawing on support from the US National Science Foundation (NSF DUE-0920350), Project MOSAIC supports a number of initiatives to help achieve these goals, including:

- *Faculty development and training opportunities,* such as the USCOTS 2011, USCOTS 2013, eCOTS 2014, eCOTS 2016, eCOTS 2018, and ICOTS 9 workshops on *Teaching Statistics Using* R *and* RStudio, our 2010 Project MO-SAIC kickoff workshop at the Institute for Mathematics and its Applications, and our *Modeling: Early and Often in Undergraduate Calculus* AMS PREP workshops offered in 2012, 2013, and 2015.
- *M-casts*, a series of regularly scheduled webinars, delivered via the Internet, that provide a forum for instructors to share their insights and innovations and to develop collaborations to refine and develop them. Recordings of M-casts are available at the Project MO-SAIC web site, http://mosaic-web.org.
- *The construction of syllabi and materials* for courses that teach MOSAIC topics in a better integrated way. Such courses and materials might be wholly new constructions, or they might be incremental modifications of existing resources that draw on the connections between the MOSAIC topics.

More details can be found at http://www.mosaic-web. org. We welcome and encourage your participation in all of these initiatives.

Computational Statistics

There are at least two ways in which statistical software can be introduced into a statistics course. In the first approach, the course is taught essentially as it was before the introduction of statistical software, but using a computer to speed up some of the calculations and to prepare higher quality graphical displays. Perhaps the size of the data sets will also be increased. We will refer to this approach as **statistical computation** since the computer serves primarily as a computational tool to replace penciland-paper calculations and drawing plots manually.

In the second approach, more fundamental changes in the course result from the introduction of the computer. Some new topics are covered, some old topics are omitted. Some old topics are treated in very different ways, and perhaps at different points in the course. We will refer to this approach as **computational statistics** because the availability of computation is shaping how statistics is done and taught. Computational statistics is a key component of **data science**, defined as the ability to use data to answer questions and communicate those results.

In practice, most courses will incorporate elements of both statistical computation and computational statistics, but the relative proportions may differ dramatically from course to course. Where on the spectrum a course lies will depend on many factors including the goals of the course, the availability of technology for student use, the perspective of the text book used, and the comfort-level of the instructor with both statistics and computation.

Among the various statistical software packages available, R is becoming increasingly popular. The recent addition of RStudio has made R both more powerful and more accessible. Because R and RStudio are free, they have become widely used in research and industry. Training in R Students need to see aspects of computation and data science early and often to develop deeper skills. Establishing precursors in introductory courses help them get started. and RStudio is often seen as an important additional skill that a statistics course can develop. Furthermore, an increasing number of instructors are using R for their own statistical work, so it is natural for them to use it in their teaching as well. At the same time, the development of R and of RStudio (an optional interface and integrated development environment for R) are making it easier and easier to get started with R.

We developed the mosaic R package (available on CRAN) to make certain aspects of statistical computation and computational statistics simpler for beginners, without limiting their ability to use more advanced features of the language. The mosaic package includes a modelling approach that uses the same general syntax to calculate descriptive statistics, create graphics, and fit linear models. Information about the mosaic package, including vignettes demonstrating features and supplementary materials (such as this book) can be found at https://cran.r-project.org/ web/packages/mosaic.

1 Introduction

In this reference book, we briefly review the commands and functions needed to analyze data from introductory and second courses in statistics. This is intended to complement the *Start Teaching with R* and *Start Modeling with R* books.

Most of our examples will use data from the HELP (Health Evaluation and Linkage to Primary Care) study: a randomized clinical trial of a novel way to link at-risk subjects with primary care. More information on the dataset can be found in chapter 14.

Since the selection and order of topics can vary greatly from textbook to textbook and instructor to instructor, we have chosen to organize this material by the kind of data being analyzed. This should make it straightforward to find what you are looking for. Some data management skills are needed by students¹. A basic introduction to key idioms is provided in Chapter 13.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses, and the mosaicData package which includes a number of data sets. The ggformula package provides support for high quality graphics using the mosaic modeling language. A paper describing the mosaic approach to teaching statistics and data science can be found at https://journal.r-project.org/archive/2017/RJ-2017-024. A short summary of the R commands needed to teach introductory statistics can be found in the mosaic package vignette: https://cran.r-project.org/web/packages/

¹ N.J. Horton, B.S. Baumer, and H. Wickham. Setting the stage for data science: integration of data management skills in introductory and second courses in statistics (http: //arxiv.org/abs/1401.3269). CHANCE, 28(2):40–50, 2015

mosaic.

Other related resources from Project MOSAIC may be helpful, including an annotated set of examples from a number of textbooks (see https://cran.r-project.org/ web/packages/mosaic/vignettes/mosaic-resources. html).

To use a package within R, it must be installed (one time), and loaded (each session). The mosaic package can be installed using the following commands:

```
> install.packages("mosaic")  # note the quotation marks
```

The # character is a comment in R, and all text after that on the current line is ignored.

Once the package is installed (one time only), it can be loaded by running the command:

> library(mosaic)

> # require(mosaic) can also be used to load packages

The RMarkdown system provides a simple markup language and renders the results in PDF, Word, or HTML. This allows students to undertake their analyses using a workflow that facilitates "reproducibility" and avoids cut and paste errors.

We typically introduce students to RMarkdown very early, requiring students to use it for assignments and reports².

RStudio features a simplified package installation tab (in the bottom right panel).

The knitr/LATEX system allows experienced users to combine R and LATEX in the same document. The reward for learning this more complicated system is much finer control over the output format. But RMarkdown is much easier to learn and is adequate even for professionallevel work.

Using Markdown or knitr/LATEX requires that the markdown package be installed.

² B.S. Baumer, M. Çetinkaya Rundel, A. Bray, L. Loi, and N. J. Horton. R Markdown: Integrating a reproducible analysis tool into introductory statistics. *Technology Innovations in Statistics Education*, 8(1):281– 283, 2014

2 Getting Started with RStudio

RStudio is an integrated development environment (IDE) for R that provides an alternative interface to R that has several advantages over other the default R interfaces:

• RStudio runs on Mac, PC, and Linux machines and provides a simplified interface that *looks and feels identical on all of them.*

The default interfaces for R are quite different on the various platforms. This is a distractor for students and adds an extra layer of support responsibility for the instructor.

• RStudio can run in a web browser.

In addition to stand-alone desktop versions or in RStudio. cloud, RStudio can be set up as a server application that is accessed via the internet.

The web interface is nearly identical to the desktop version. As with other web services, users login to access their account. If students logout and login in again later, even on a different machine, their session is restored and they can resume their analysis right where they left off. With a little advanced set up, instructors can save the history of their classroom R use and students can load those history files into their own environment.

 RStudio provides support for reproducible research. RStudio makes it easy to include text, statistical analysis (R code and R output), and graphical displays all in the same document. The RMarkdown system provides a simple markup language and renders the results in HTML. The knitr/LATEX system allows users A series of getting started videos are available at https://nhorton.people. amherst.edu/rstudio.

CAUTION!

The desktop and server version of RStudio are so similar that if you run them both, you will have to pay careful attention to make sure you are working in the one you intend to be working in.

Note

Using RStudio in a browser is like Facebook for statistics. Each time the user returns, the previous session is restored and they can resume work where they left off. Users can login from any device with internet access. to combine R and LATEX in the same document. The reward for learning this more complicated system is much finer control over the output format. Depending on the level of the course, students can use either of these for homework and projects.

- RStudio provides an integrated support for editing and executing R code and documents.
- RStudio provides some useful functionality via a graphical user interface.

RStudio is not a GUI for R, but it does provide a GUI that simplifies things like installing and updating packages; monitoring, saving and loading environments; importing and exporting data; browsing and exporting graphics; and browsing files and documentation.

• RStudio provides access to the manipulate package. The manipulate package provides a way to create simple interactive graphical applications quickly and easily.

While one can certainly use R without using RStudio, RStudio makes a number of things easier and we highly recommend using RStudio. Furthermore, since RStudio is in active development, we fully expect more useful features in the future.

We primarily use an online version of RStudio. RStudio is a innovative and powerful interface to R that runs in a web browser or on your local machine. Running in the browser has the advantage that you don't have to install or configure anything. Just login and you are good to go. Furthermore, RStudio will "remember" what you were doing so that each time you login (even on a different machine) you can pick up right where you left off. This is "R in the cloud" and works a bit like GoogleDocs or Facebook for R.

R can also be obtained from http://cran.r-project. org/. Download and installation are pretty straightforward for Mac, PC, or Linux machines. RStudio is available from http://www.rstudio.org/. To use Markdown or knitr/LATEX requires that the knitr package be installed on your system.

2.1 Connecting to an RStudio server

RStudio servers have been set up at a number of schools to facilitate cloud-based computing.

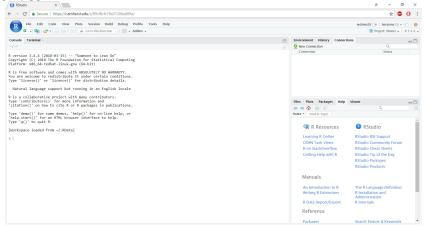
Once you connect to the server, you should see a login screen:

🔿 🔘 🚺 RStudio Sign In 🛛 🗙		
$\dot{-} \rightarrow \mathbf{C}$ \triangleq https://r.amherst.edu	u/auth-sign-in	
Rstudio		
	Sign in to RStudio	
	Username:	
	Password:	
	Stay signed in	
	Sign In	

RStudio servers have been installed at many institutions. More details about (free) academic licenses for RStudio Server Pro as well as setup instructions can be found at http://www.rstudio.com/ resources/faqs under the Academic tab.

The RStudio server doesn't tend to work well with Internet Explorer.

Once you authenticate, you should see the RStudio interface:



Notice that RStudio divides its world into four panels. Several of the panels are further subdivided into multiple tabs. Which tabs appear in which panels can be customized by the user.

R can do much more than a simple calculator, and we

will introduce additional features in due time. But performing simple calculations in R is a good way to begin learning the features of RStudio.

Commands entered in the Console tab are immediately executed by R. A good way to familiarize yourself with the console is to do some simple calculator-like computations. Most of this will work just like you would expect from a typical calculator. Try typing the following commands in the console panel.

> 5 + 3	
[1] 8	
> 15.3 * 23.4	
[1] 358.02	
> sqrt (16)	# square root
[1] 4	

This last example demonstrates how functions are called within R as well as the use of comments. Comments are prefaced with the # character. Comments can be very helpful when writing scripts with multiple commands or to annotate example code for your students.

You can save values to named variables for later reuse.

```
> product = 15.3 * 23.4  # save result
> product  # display the result  using one
right-to-le
tors rathe
and forth
operator
> product <- 15.3 * 23.4  # <- can be used instead of
> product [1] 358.02  # <- can be used instead of
[1] 358.02  # the result  the use of the use
```

Once variables are defined, they can be referenced in other operations and functions.

It's probably best to settle on using one or the other of the right-to-left assignment operators rather than to switch back and forth. We prefer the arrow operator because it represents visually what is happening in an assignment and because it makes a clear distinction between the assignment operator, the use of = to provide values to arguments of functions, and the use of == to test for equality.

The semi-colon can be used to place multiple commands on one line. One frequent use of this is to save and print a value all in one go:

> product <- 15.3 * 23.4; product # save result and show it</pre>

[1] 358.02

2.1.1 Version information

At times it may be useful to check what version of the mosaic package, R, and RStudioyou are using. Running sessionInfo() will display information about the version of R and packages that are loaded and RStudio.Version() will provide information about the version of RStudio.

```
> sessionInfo()
R version 3.5.0 (2018-04-23)
Platform: x86_64-apple-darwin15.6.0 (64-bit)
Running under: macOS Sierra 10.12.6
Matrix products: default
BLAS: /Library/Frameworks/R.framework/Versions/3.5/Resources/lib/libRblas.0.dylib
```

```
LAPACK: /Library/Frameworks/R.framework/Versions/3.5/Resources/lib/libRlapack.dylib
locale:
[1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
attached base packages:
                        graphics grDevices utils
[1] grid
              stats
                                                       datasets
[7] methods
              base
other attached packages:
[1] mosaic_1.2.0
                       Matrix_1.2-14
                                          mosaicData_0.16.0
[4] ggformula_0.7.9003 ggplot2_2.2.1.9000 dplyr_0.7.5
[7] lattice_0.20-35
                       knitr_1.20
loaded via a namespace (and not attached):
 [1] Rcpp_0.12.17
                      highr_0.7
                                       pillar_1.2.3
 [4] compiler_3.5.0
                      plyr_1.8.4
                                       bindr_0.1.1
 [7] tools_3.5.0
                      evaluate_0.10.1 tibble_1.4.2
[10] gtable_0.2.0
                      nlme_3.1-137
                                       pkgconfig_2.0.1
[13] rlang_0.2.1
                      psych_1.8.4
                                       parallel_3.5.0
[16] ggdendro_0.1-20
                      bindrcpp_0.2.2
                                       gridExtra_2.3
[19] withr_2.1.2
                      stringr_1.3.1
                                       tidyselect_0.2.4
[22] mosaicCore_0.5.0 glue_1.2.0
                                       R6_2.2.2
[25] foreign_0.8-70
                      reshape2_1.4.3
                                       purrr_0.2.5
[28] tidyr_0.8.1
                      magrittr_1.5
                                       scales_0.5.0
                                       assertthat_0.2.0
[31] MASS_7.3-50
                      splines_3.5.0
[34] mnormt_1.5-5
                      colorspace_1.3-2 stringi_1.2.3
[37] lazyeval_0.2.1
                      munsell_0.5.0
                                       broom_0.4.4
```

2.2 Working with Files

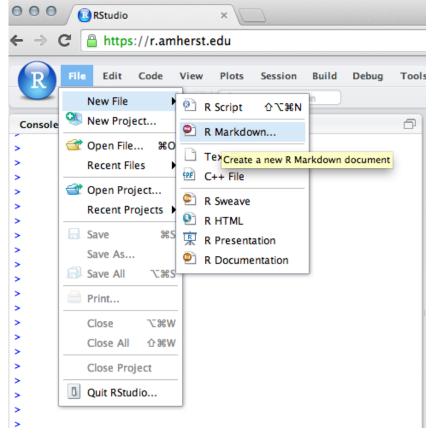
2.2.1 Working with R Script Files

As an alternative, R commands can be stored in a file. RStudio provides an integrated editor for editing these files and facilitates executing some or all of the commands. To create a file, select File, then New File, then R Script from the RStudio menu. A file editor tab will open in the Source panel. R code can be entered here, and buttons and menu items are provided to run all the code (called sourcing the file) or to run the code on a single line or in a selected section of the file.

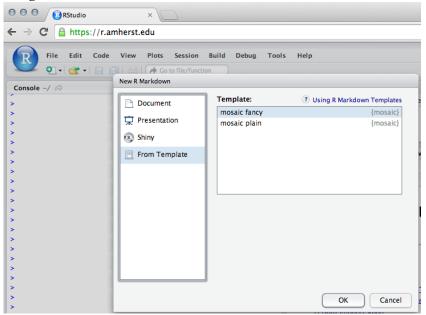
2.2.2 Working with RMarkdown, and knitr/ETFX

A third alternative is to take advantage of RStudio's support for reproducible research. If you already know LATEX, you will want to investigate the knitr/LATEX capabilities. For those who do not already know LATEX, the simpler RMarkdown system provides an easy entry into the world of reproducible research methods. It also provides a good facility for students to create homework and reports that include text, R code, R output, and graphics.

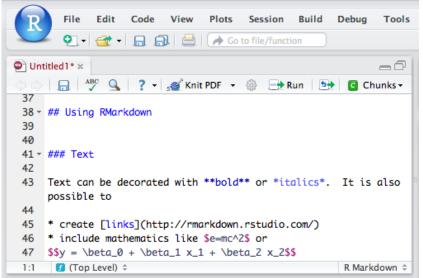
To create a new RMarkdown file, select File, then New File, then RMarkdown. The file will be opened with a short template document that illustrates the mark up language.



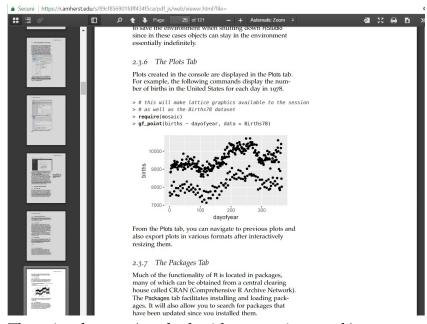
The mosaic package includes two useful RMarkdown templates for getting started: fancy includes bells and whistles (and is intended to give an overview of features), while plain is useful as a starting point for a new analysis. These are accessed using the Template option when creating a new RMarkdown file.



Click on the Knit button to convert to an HTML, PDF, or Word file.



This will generate a formatted version of the document.



There is a button (marked with a question mark) which provides a brief description of the supported markup commands. The RStudio web site includes more extensive tutorials on using RMarkdown.

It is important to remember that unlike R scripts, which are executed in the console and have access to the console environment, RMarkdown and knitr/IATEX files do not have access to the console environment This is a good feature because it forces the files to be selfcontained, which makes them transferable and respects good reproducible research practices. But beginners, especially if they adopt a strategy of trying things out in the console and copying and pasting successful code from the console to their file, will often create files that are incomplete and therefore do not compile correctly.

2.3 The Other Panels and Tabs

2.3.1 The History Tab

As commands are entered in the console, they appear in the History tab. These histories can be saved and loaded, there is a search feature to locate previous commands, and individual lines or sections can be transferred back to the console. Keeping the History tab open will allow you CAUTION! RMarkdown, and knitr/LATEX files do not have access to the console environment, so the code in them must be selfcontained. to go back and see the previous several commands. This can be especially useful when commands produce a fair amount of output and so scroll off the screen rapidly.

2.3.2 Communication between tabs

RStudio provides several ways to move R code between tabs. Pressing the Run button in the editing panel for an R script or RMarkdown or other file will copy lines of code into the Console and run them.

2.3.3 The Files Tab

The Files tab provides a simple file manager. It can be navigated in familiar ways and used to open, move, rename, and delete files. In the browser version of RStudio, the Files tab also provides a file upload utility for moving files from the local machine to the server. In RMarkdown and knitr files one can also run the code in a particular chunk or in all of the chunks in a file. Each of these features makes it easy to try out code "live" while creating a document that keeps a record of the code.

In the reverse direction, code from the history can be copied either back into the console to run them again (perhaps after editing) or into one of the file editing tabs for inclusion in a file.

2.3.4 The Help Tab

The Help tab is where RStudio displays R help files. These can be searched and navigated in the Help tab. You can also open a help file using the ? operator in the console. For example the following command will provide the help file for the logarithm function.

> ?log

2.3.5 The Environment Tab

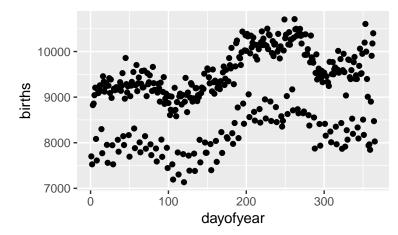
The Environment tab shows the objects available to the console. These are subdivided into data, values (non-

dataframe, non-function objects) and functions. The broom icon can be used to remove all objects from the environment, and it is good to do this from time to time, especially when running in RStudio server or if you choose to save the environment when shutting down RStudio since in these cases objects can stay in the environment essentially indefinitely.

2.3.6 The Plots Tab

Plots created in the console are displayed in the Plots tab. For example, the following commands display the number of births in the United States for each day in 1978.

```
> library(mosaic)
> gf_point(births ~ dayofyear, data = Births78)
```



From the Plots tab, you can navigate to previous plots and also export plots in various formats after interactively resizing them.

2.3.7 The Packages Tab

Much of the functionality of R is located in packages, many of which can be obtained from a central clearing house called CRAN (Comprehensive R Archive Network). The Packages tab facilitates installing and loading packages. It will also allow you to search for packages that have been updated since you installed them.

3 One Quantitative Variable

3.1 Numerical summaries

R includes a number of commands to numerically summarize variables. These include the capability of calculating the mean, standard deviation, variance, median, five number summary, interquartile range (IQR) as well as arbitrary quantiles. We will illustrate these using the CESD (Center for Epidemiologic Studies–Depression) measure of depressive symptoms (which takes on values between o and 60, with higher scores indicating more depressive symptoms).

To improve the legibility of output, we will also set the default number of digits to display to a more reasonable level (see <code>?options()</code> for more configuration possibilities).

```
> library(mosaic)
> options(digits = 4)
> mean(~ cesd, data = HELPrct)
[1] 32.85
```

Note that the mean() function in the mosaic package supports a formula interface common to lattice graphics and linear models (e.g., lm()). The mosaic package provides many other functions that use the same notation, which we will be using throughout this document.

The same output could be created using the following commands (though we will use the MOSAIC versions when available). DIGGING DEEPER If you have not seen the formula notation before, the companion book, *Start Teaching with R* provides a detailed presentation. *Start Modeling with R*, another companion book, details the relationship between the process of modeling and the formula notation.

```
> with(HELPrct, mean(cesd))
[1] 32.85
> mean(HELPrct$cesd)
```

[1] 32.85

Similar functionality exists for other summary statistics.

```
> sd(~ cesd, data = HELPrct)
[1] 12.51
```

```
> sd(~ cesd, data = HELPrct)^2
[1] 156.6
> var(~ cesd, data = HELPrct)
[1] 156.6
```

It is also straightforward to calculate quantiles of the distribution.

```
> median(~ cesd, data = HELPrct)
```

[1] 34

By default, the quantile() function displays the quartiles, but can be given a vector of quantiles to display.

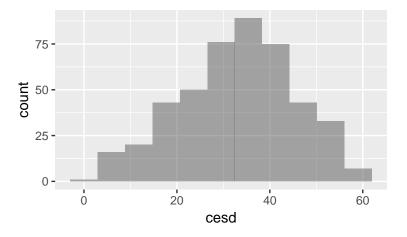
CAUTION! Not all commands have been upgraded to support the formula interface. For these functions, variables within dataframes must be accessed using with() or the \$ operator. Finally, the favstats() function in the mosaic package provides a concise summary of many useful statistics.

```
> favstats(~ cesd, data = HELPrct)
min Q1 median Q3 max mean sd n missing
1 25 34 41 60 32.85 12.51 453 0
```

3.2 Graphical summaries

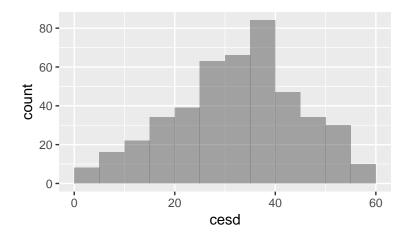
The gf_histogram() function is used to create a histogram. Here we use the formula interface (as discussed in the *Start Modeling with R* book) to specify that we want a histogram of the CESD scores.

```
> gf_histogram(~ cesd, data = HELPrct, binwidth = 5.9)
```



We can use the **binwidth()** and **center()** options to control the location of the bins.

> gf_histogram(~ cesd, data = HELPrct, binwidth = 5, center = 2.5)



In the HELPrct dataset, approximately one quarter of the subjects are female.

```
> tally(~ sex, data = HELPrct)
sex
female male
    107 346
> tally(~ sex, format = "percent", data = HELPrct)
sex
female male
    23.62 76.38
```

It is straightforward to restrict our attention to just the female subjects. If we are going to do many things with a subset of our data, it may be easiest to make a new dataframe containing only the cases we are interested in. The filter() function in the dplyr package can be used to generate a new dataframe containing just the women or just the men (see also section 13.5). Once this is created, the the stem() function is used to create a stem and leaf plot.

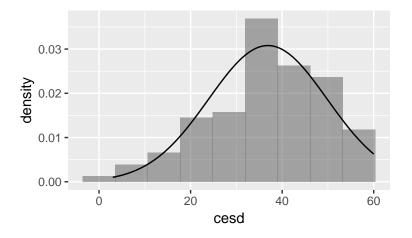
```
> Female <- filter(HELPrct, sex == 'female')
> Male <- filter(HELPrct, sex == 'male')
> with(Female, stem(cesd))
```

CAUTION! Note that the tests for equality use *two* equal signs

The decimal point is 1 digit(s) to the right of the |

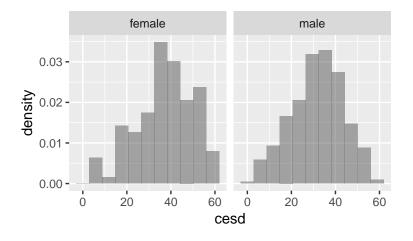
0	3
0	567
1	3
1	555589999
2	123344
2	66889999
3	0000233334444
3	5556666777888899999
4	00011112222334
4	555666777889
5	011122222333444
5	67788
6	Θ

Subsets can also be generated and used "on the fly" (this time including an overlaid normal density):



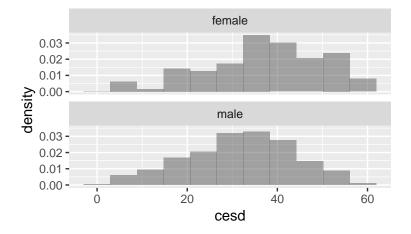
Alternatively, we can make side-by-side plots to compare multiple subsets.

```
> gf_dhistogram(~ cesd, data = HELPrct, binwidth = 5.9) %>%
gf_facet_wrap(~ sex)
```



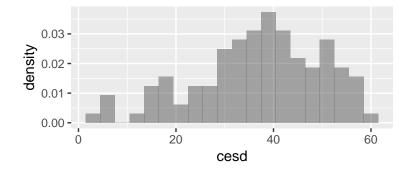
The layout can be rearranged.

```
> gf_dhistogram(~ cesd, data = HELPrct, binwidth = 5.9) %>%
gf_facet_wrap(~ sex, nrow = 2)
```



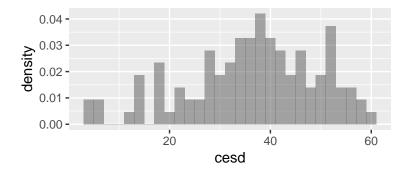
We can control the number of bins in a number of ways. These can be specified as the total number.

> gf_dhistogram(~ cesd, bins = 20, data = Female)

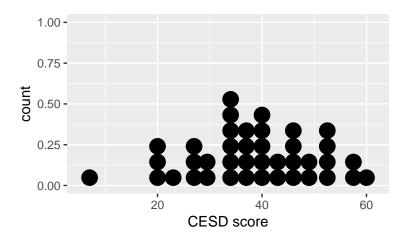


The width of the bins can be specified.

```
> gf_dhistogram(~ cesd, binwidth = 2, data = Female)
```



The gf_dotplot() function is used to create a dotplot for a smaller subset of subjects (homeless females). We also demonstrate how to change the x-axis label.

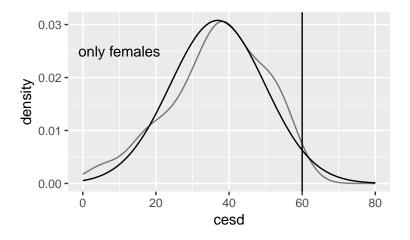


3.3 Density curves

One disadvantage of histograms is that they can be sensitive to the choice of the number of bins. Another display to consider is a density curve.

Here we adorn a density plot with some additions to demonstrate how to build up a graphic for pedagogical purposes. We add some text, a superimposed normal density as well as a vertical line. A variety of line types and colors can be specified, as well as line widths. Density plots are also sensitive to certain choices. If your density plot is too jagged or too smooth, try changing the adjust argument: larger than 1 for smoother plots, less than 1 for more jagged plots.

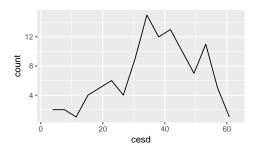
DIGGING DEEPER The plotFun() function can also be used to annotate plots (see section 10.2.1).



3.4 Frequency polygons

A third option is a frequency polygon, where the graph is created by joining the midpoints of the top of the bars of a histogram.

> gf_freqpoly(~ cesd, data = Female, binwidth = 3.8)



3.5 Normal distributions

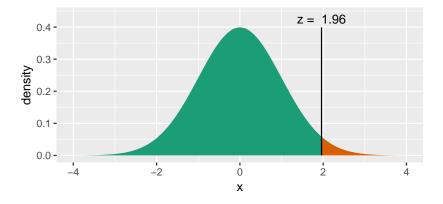
The most famous density curve is a normal distribution. The xpnorm() function displays the probability that a random variable is less than the first argument, for a normal distribution with mean given by the second argument and standard deviation by the third. More information about probability distributions can be found in section 11.

x is for eXtra.

> xpnorm(1.96, mean = 0, sd = 1)

If X ~ N(0, 1), then P(X <= 1.96) = P(Z <= 1.96) = 0.975 P(X > 1.96) = P(Z > 1.96) = 0.025

[1] 0.975



3.6 Inference for a single sample

We can calculate a 95% confidence interval for the mean CESD score for females by using a t-test:

```
> t.test(~ cesd, data = Female)
One Sample t-test
data: cesd
t = 29, df = 110, p-value <2e-16
alternative hypothesis: true mean is not equal to 0
95 percent confidence interval:
34.39 39.38
sample estimates:
mean of x
36.89
> confint(t.test(~ cesd, data = Female))
mean of x lower upper level
1 36.89 34.39 39.38 0.95
```

But it's also straightforward to calculate this using a bootstrap. The statistic that we want to resample is the mean.

```
> mean(~ cesd, data = Female)
[1] 36.89
```

One resampling trial can be carried out:

```
> mean(~ cesd, data = resample(Female))
```

[1] 39.15

Another will yield different results:

```
> mean(~ cesd, data = resample(Female))
```

[1] 36.03

Now conduct 1000 resampling trials, saving the results in an object called trials:

```
> trials <- do(1000) * mean(~ cesd, data = resample(Female))
> head(trials, 3)
            mean
1 36.72
2 37.70
3 34.93
> qdata(~ mean, c(.025, .975), data = trials)
            quantile            p
2.5% 34.27 0.025
97.5% 39.38 0.975
```

DIGGING DEEPER More details and examples can be found in the mosaic package Resampling Vignette.

Here we sample with replacement from the original dataframe, creating a resampled dataframe with the same number of rows.

Even though a single trial is of little use, it's smart having students do the calculation to show that they are (usually!) getting a different result than without resampling.

4 One Categorical Variable

4.1 Numerical summaries

The tally() function can be used to calculate counts, percentages and proportions for a categorical variable.

```
> tally(~ homeless, data = HELPrct)
homeless
homeless
           housed
     209
              244
> tally(~ homeless, margins = TRUE, data = HELPrct)
homeless
homeless
           housed
                     Total
     209
              244
                       453
> tally(~ homeless, format = "percent", data = HELPrct)
homeless
homeless
           housed
   46.14
            53.86
> tally(~ homeless, format = "proportion", data = HELPrct)
homeless
homeless
           housed
  0.4614
           0.5386
```

DIGGING DEEPER The *Start Teaching with R* companion book introduces the formula notation used throughout this book. See also *Start Teaching with R* for the connections to statistical modeling.

4.2 The binomial test

An exact confidence interval for a proportion (as well as a test of the null hypothesis that the population proportion is equal to a particular value [by default 0.5]) can be calculated using the binom.test() function. The standard binom.test() requires us to tabulate.

The mosaic package provides a formula interface that avoids the need to pre-tally the data.

```
> result <- binom.test(~ (homeless == "homeless"), data = HELPrct)
> result
```

```
data: HELPrct$(homeless == "homeless") [with success = TRUE]
number of successes = 210, number of trials = 450, p-value =
0.1
alternative hypothesis: true probability of success is not equal to 0.5
95 percent confidence interval:
0.4147 0.5085
sample estimates:
probability of success
0.4614
```

As is generally the case with commands of this sort, there are a number of useful quantities available from the object returned by the function. > names(result)
[1] "statistic" "parameter" "p.value" "conf.int"
[5] "estimate" "null.value" "alternative" "data.name"

These can be extracted using the \$ operator or an extractor function. For example, the user can extract the confidence interval or p-value.

4.3 The proportion test

A similar interval and test can be calculated using the function prop.test(). Here is a count of the number of people at each of the two levels of homeless

```
> tally(~ homeless, data = HELPrct)
homeless
homeless housed
```

244

209

The prop.test() function will carry out the calcula-

tions of the proportion test and report the result.

DIGGING DEEPER Most of the objects in R have a print() method. So when we get result, what we are seeing displayed in the console is print(result). There may be a good deal of additional information lurking inside the object itself.

In some situations, such as graphics, the object is returned *invisibly*, so nothing prints. That avoids your having to look at a long printout not intended for human consumption. You can still assign the returned object to a variable and process it later, even if nothing shows up on the screen. This is sometimes helpful for lattice graphics functions.

```
1-sample proportions test without continuity correction
data: HELPrct$(homeless == "homeless") [with success = TRUE]
X-squared = 2.7, df = 1, p-value = 0.1
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
    0.4160 0.5074
sample estimates:
    p
0.4614
```

In this statement, prop.test is examining the homeless variable in the same way that tally() would. The prop.test() function can also work directly with numerical counts, the way binom.test() does.

```
> prop.test(209, 209 + 244, correct = FALSE)
```

1-sample proportions test without continuity correction

```
data: 209 out of 209 + 244
X-squared = 2.7, df = 1, p-value = 0.1
alternative hypothesis: true p is not equal to 0.5
95 percent confidence interval:
    0.4160 0.5074
sample estimates:
    p
0.4614
```

MORE INFO We write homeless == "homeless" to define unambiguously which proportion we are considering. We could also have written homeless == "housed".

prop.test() calculates a Chisquared statistic. Most introductory texts use a z-statistic. They are mathematically equivalent in terms of inferential statements, but you may need to address the discrepancy with your students.

4.4 Goodness of fit tests

A variety of goodness of fit tests can be calculated against a reference distribution. For the HELP data, we could test the null hypothesis that there is an equal proportion of subjects in each substance abuse group back in the original populations.

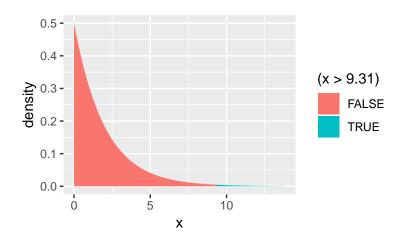
```
> tally(~ substance, format = "percent", data = HELPrct)
substance
alcohol cocaine heroin
39.07 33.55 27.37
```

```
> observed <- tally(~ substance, data = HELPrct)</pre>
> observed
substance
alcohol cocaine heroin
    177
             152
                      124
                                                                             CAUTION!
                                                                   In addition to the format op-
                                                                   tion, there is an option margins
                                                                   to include marginal totals in the
                                                                   table. The default in tally() is
> p <- c(1/3, 1/3, 1/3)
                            # equivalent to rep(1/3, 3)
                                                                   margins = FALSE. Try it out!
> chisq.test(observed, p = p)
Chi-squared test for given probabilities
data: observed
X-squared = 9.3, df = 2, p-value = 0.01
> total <- sum(observed)</pre>
> total
[1] 453
> expected <- total*p</pre>
> expected
[1] 151 151 151
```

We can also calculate the χ^2 statistic manually, as a function of observed and expected values.

```
> chisq <- sum((observed - expected)^2/(expected))
> chisq
[1] 9.311
> 1 - pchisq(chisq, df = 2)
[1] 0.009508
```

It may be helpful to consult a graph of the statistic, where the shaded area represents the value to the right of the observed value. The pchisq() function calculates the probability that a χ^2 random variable with df() degrees is freedom is less than or equal to a given value. Here we calculate the complement to find the area to the right of the observed Chi-square statistic. > gf_dist("chisq", df = 2, fill = ~ (x > 9.31), geom = "area")



```
Alternatively, the mosaic package provides a version of chisq.test() with more verbose output.
```

```
> xchisq.test(observed, p = p)
```

```
Chi-squared test for given probabilities

data: x

X-squared = 9.3, df = 2, p-value = 0.01

177 152 124

(151.00) (151.00) (151.00)

[4.4768] [0.0066] [4.8278]

< 2.116> < 0.081> <-2.197>

key:

observed

(expected)

[contribution to X-squared]

<Pearson residual>
```

> # clean up variables no longer needed > rm(observed, p, total, chisq) x in xchisq.test() stands for eXtra.

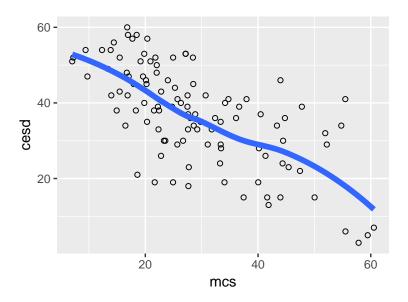
Objects in the workspace are listed in the ENVIRONMENT tab in RStudio. If you want to clean up that listing, remove objects that are no longer needed with rm().

5 Two Quantitative Variables

5.1 Scatterplots

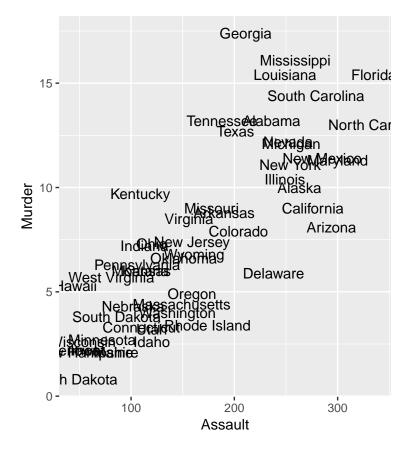
We always encourage students to start any analysis by graphing their data. Here we augment a scatterplot of the CESD (a measure of depressive symptoms, higher scores indicate more symptoms) and the MCS (mental component score from the SF-36, where higher scores indicate better functioning) for female subjects with a lowess (locally weighted scatterplot smoother) line, using a circle as the plotting character and slightly thicker line.

```
> Female <- filter(HELPrct, female == 1)
> gf_point(cesd ~ mcs, data = Female, shape = 1) %>%
gf_smooth(se = FALSE, size = 2)
```



The lowess line can help to assess linearity of a relationship. This is added by specifying both points (using 'p') and a lowess smoother. It's straightforward to plot something besides a character in a scatterplot. In this example, the USArrests can be used to plot the association between murder and assault rates, with the state name displayed.

```
> gf_text(Murder ~ Assault,
    label = ~ rownames(USArrests),
    data = USArrests)
```



DIGGING DEEPER The *Start Modeling with R* companion book will be helpful if you are unfamiliar with the modeling language. The *Start Teaching with R* also provides useful guidance in getting started.

5.2 Correlation

Correlations can be calculated for a pair of variables, or for a matrix of variables.

> cor(cesd ~ mcs, data = Female)
[1] -0.6738
> smallHELP <- select(Female, cesd, mcs, pcs)
> cor(smallHELP)

cesdmcspcscesd1.0000-0.6738-0.3685mcs-0.67381.00000.2664pcs-0.36850.26641.0000

By default, Pearson correlations are provided. Other variants (e.g., Spearman) can be specified using the method option.

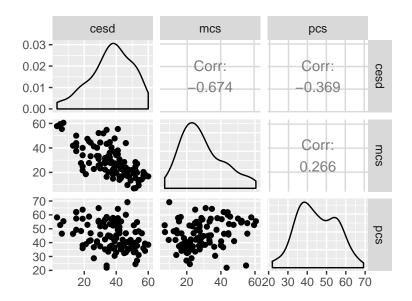
```
> cor(cesd ~ mcs, method = "spearman", data = Female)
[1] -0.6662
```

5.3 Pairs plots

A pairs plot (scatterplot matrix) can be calculated for each pair of a set of variables.

- > library(GGally)
- > ggpairs(smallHELP)

The GGally package has support for more elaborate pairs plots.



5.4 Simple linear regression

Linear regression models are described in detail in *Start Modeling with R*. These use the same formula interface introduced previously for numerical and graphical summaries to specify the outcome and predictors. Here we consider fitting the model cesd \sim mcs.

```
> cesdmodel <- lm(cesd ~ mcs, data = Female)
> coef(cesdmodel)
(Intercept) mcs
57.349 -0.707
```

To simplify the output, we turn off the option to display significance stars.

```
> options(show.signif.stars = FALSE)
> coef(cesdmodel)
(Intercept) mcs
57.349 -0.707
> msummary(cesdmodel)
Estimate Std. Error t value Pr(>|t|)
(Intercept) 57.3485 2.3806 24.09 < 2e-16
mcs -0.7070 0.0757 -9.34 1.8e-15</pre>
```

Residual standard error: 9.66 on 105 degrees of freedom Multiple R-squared: 0.454,Adjusted R-squared: 0.449 F-statistic: 87.3 on 1 and 105 DF, p-value: 1.81e-15

```
> coef(summary(cesdmodel))
```

Estimate Std. Error t value Pr(>|t|) (Intercept) 57.349 2.38062 24.090 1.425e-44 mcs -0.707 0.07566 -9.344 1.813e-15

```
> confint(cesdmodel)
```

2.5 % 97.5 % (Intercept) 52.6282 62.069 mcs -0.8571 -0.557

```
> rsquared(cesdmodel)
```

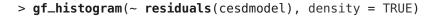
[1] 0.454

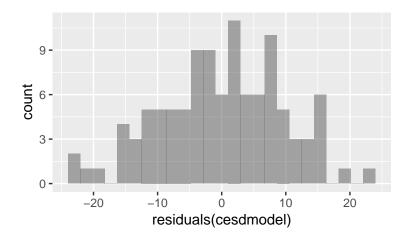
We tend to introduce linear regression early in our courses, as a purely descriptive technique.

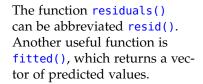
It's important to pick good names for modeling objects. Here the output of lm() is saved as cesdmodel, which denotes that it is a regression model of depressive symptom scores. > class(cesdmodel)

[1] "lm"

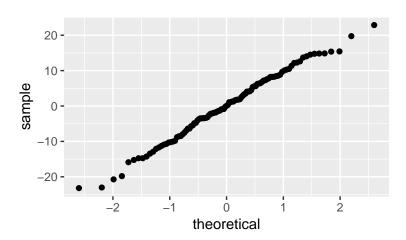
The return value from lm() is a linear model object. A number of functions can operate on these objects, as seen previously with coef(). The function residuals() returns a vector of the residuals.

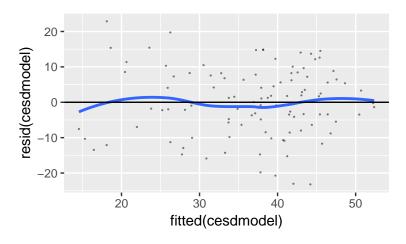






> gf_qq(~ resid(cesdmodel))

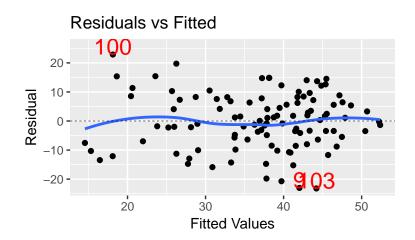




The mplot() function can facilitate creating a variety of useful plots, including the same residuals vs. fitted scatterplots, by specifying the which = 1 option.

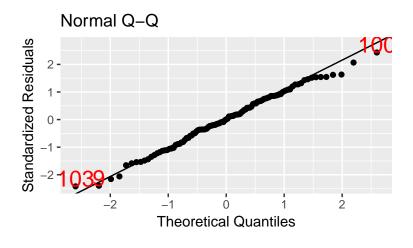
```
> mplot(cesdmodel, which = 1)
```

[[1]]



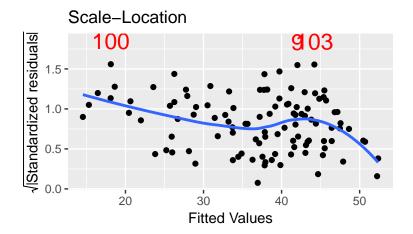
It can also generate a normal quantile-quantile plot (which = 2),

> mplot(cesdmodel, which = 2)



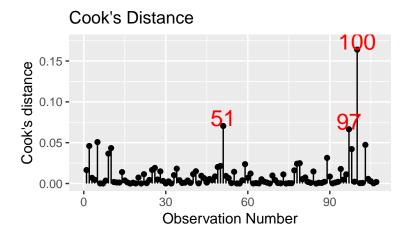
scale vs. location,

> mplot(cesdmodel, which = 3)



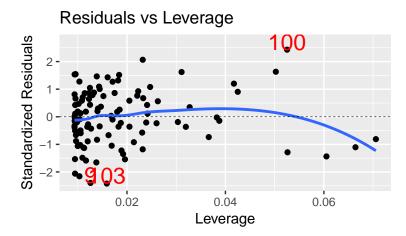
Cook's distance by observation number,

> mplot(cesdmodel, which = 4)



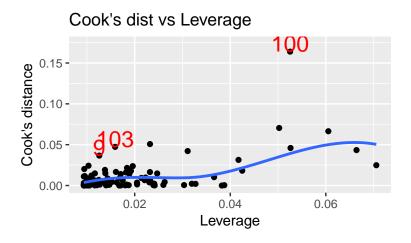
residuals vs. leverage,

> mplot(cesdmodel, which = 5)



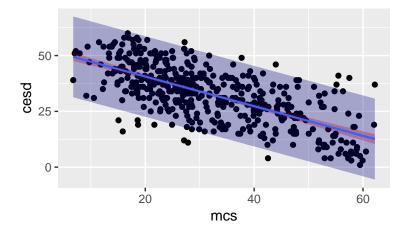
and Cook's distance vs. leverage.

> mplot(cesdmodel, which = 6)



Prediction intervals can be added to a plot using the interval option in $gf_lm()$.

```
> gf_point(cesd ~ mcs, data = HELPrct) %>%
    gf_lm(interval = "confidence", fill = "red") %>%
    gf_lm(interval = "prediction", fill = "navy")
```



6 *Two Categorical Variables*

6.1 Cross classification tables

Cross classification (two-way or *R* by *C*) tables can be constructed for two (or more) categorical variables. Here we consider the contingency table for homeless status (homeless one or more nights in the past 6 months or housed) and sex.

We can also calculate column percentages:

We can calculate the odds ratio directly from the table:

> OR <- (40/169)/(67/177) > OR [1] 0.6253

The mosaic package has a function which will calculate odds ratios:

[1] 0.6253

The CrossTable() function in the gmodels package also displays a cross classification table.

```
> library(gmodels)
> with(HELPrct, CrossTable(homeless, sex,
    prop.r = FALSE, prop.chisq = FALSE, prop.t = FALSE))
```

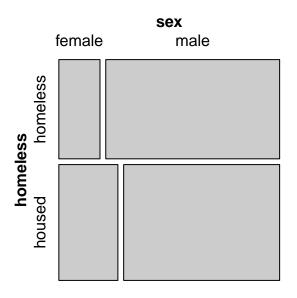
```
Cell Contents
|-----|
| N |
| N / Col Total |
|------
```

Total Observations in Table: 453

	sex		
homeless	female	male	Row Total
homeless	40	169	209
	0.374	0.488	
housed	67	177	244
	0.626	0.512	
Column Total	107	346	453
	0.236	0.764	I

Graphical summaries of cross classification tables may be helpful in visualizing associations. Mosaic plots are one example, where the total area (all observations) is proportional to one. Here we see that males tend to be over-represented amongst the homeless subjects (as represented by the horizontal line which is higher for the homeless rather than the housed).

```
> vcd::mosaic(mytab)
```

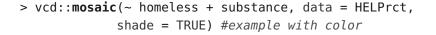


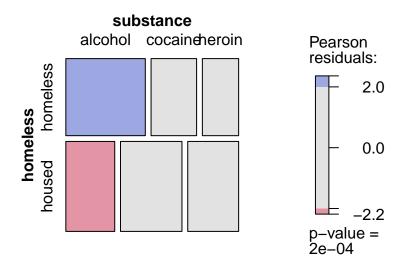
CAUTION!

The jury is still out regarding the utility of mosaic plots (also known as eikosograms), due to their low data to ink ratio. We have found them to be helpful to reinforce understanding of a two way contingency table.

E. R. Tufte. *The Visual Display of Quantitative Information*. Graphics Press, Cheshire, CT, 2nd edition, 2001

The mosaic() function in the vcd package makes mosaic plots.





6.2 Creating tables from summary statistics

Tables can be created from summary statistics using the do() function.

6.3 *Chi-squared tests*

```
> chisq.test(tally(~ homeless + sex, margins = FALSE,
    data = HELPrct), correct = FALSE)
Pearson's Chi-squared test
data: tally(~homeless + sex, margins = FALSE, data = HELPrct)
X-squared = 4.3, df = 1, p-value = 0.04
```

There is a statistically significant association found: it is unlikely that we would observe an association this strong if homeless status and sex were independent in the population.

When a student finds a significant association, it's important for them to be able to interpret this in the context of the problem. The xchisq.test() function provides additional details (observed, expected, contribution to statistic, and residual) to help with this process.

x is for eXtra.

Pearson's Chi-squared test data: x X-squared = 4.3, df = 1, p-value = 0.04 40 169 (49.37) (159.63) [1.78][0.55] <-1.33> < 0.74> 67 177 (57.63) (186.37)[1.52] [0.47] < 1.23> <-0.69> key: observed (expected)

[contribution to X-squared]
<Pearson residual>

We observe that there are fewer homeless women, and more homeless men that would be expected.

6.4 Fisher's exact test

An exact test can also be calculated. This is computationally straightforward for 2 by 2 tables. Options to help constrain the size of the problem for larger tables exist (see ?fisher.test()).

DIGGING DEEPER Note the different estimate of the odds ratio from that seen in section 6.1. The fisher.test() function uses a different estimator (and different interval based on the profile likelihood).

```
Fisher's Exact Test for Count Data
```

```
data: tally(~homeless + sex, margins = FALSE, data = HELPrct)
p-value = 0.05
alternative hypothesis: true odds ratio is not equal to 1
95 percent confidence interval:
    0.3895 0.9968
sample estimates:
    odds ratio
        0.6259
```

7 Quantitative Response, Categorical Predictor

7.1 *A dichotomous predictor: numerical and graphical summaries*

Here we will compare the distributions of CESD scores by sex. The mean() function can be used to calculate the mean CESD score separately for males and females.

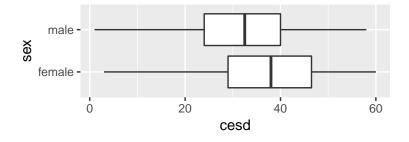
```
> mean(cesd ~ sex, data = HELPrct)
female male
36.89 31.60
```

The favstats() function can provide more statistics by group.

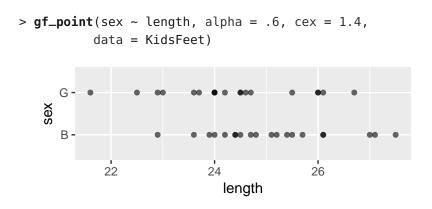
```
> favstats(cesd ~ sex, data = HELPrct)
        sex min Q1 median Q3 max mean sd n missing
1 female 3 29 38.0 46.5 60 36.89 13.02 107 0
2 male 1 24 32.5 40.0 58 31.60 12.10 346 0
```

Boxplots are a particularly helpful graphical display to compare distributions. The gf_boxplot() function can be used to display the boxplots for the CESD scores separately by sex. We see from both the numerical and graphical summaries that women tend to have slightly higher CESD scores than men. Although we usually put explanatory variables along the horizontal axis, page layout sometimes makes the other orientation preferable for these plots.

```
> gf_boxplot(cesd ~ sex, data = HELPrct) %>%
gf_refine(coord_flip())
```



When sample sizes are small, there is no reason to summarize with a boxplot since gf_point() can handle categorical predictors. Even with 10–20 observations in a group, a scatter plot is often quite readable. Setting the alpha level helps detect multiple observations with the same value.



One of us once saw a biologist proudly present side-by-side boxplots. Thinking a major victory had been won, he naively asked how many observations were in each group. "Four," replied the biologist.

7.2 A dichotomous predictor: two-sample t

The Student's two sample t-test can be run without (default) or with an equal variance assumption.

```
> t.test(cesd ~ sex, var.equal = FALSE, data = HELPrct)
Welch Two Sample t-test
data: cesd by sex
t = 3.7, df = 170, p-value = 3e-04
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
```

2.493 8.087 sample estimates: mean in group female mean in group male 36.89 31.60

We see that there is a statistically significant difference between the two groups.

We can repeat using the equal variance assumption.

> t.test(cesd ~ sex, var.equal = TRUE, data = HELPrct)

Two Sample t-test

The groups can also be compared using the lm() function (also with an equal variance assumption). The mosaic command msummary() provides a slightly terser version of the typical output from summary().

```
> msummary(lm(cesd ~ sex, data = HELPrct))
Estimate Std. Error t value Pr(>|t|)
(Intercept) 36.89 1.19 30.96 < 2e-16
sexmale -5.29 1.36 -3.88 0.00012</pre>
```

Residual standard error: 12.3 on 451 degrees of freedom Multiple R-squared: 0.0323,Adjusted R-squared: 0.0302 F-statistic: 15.1 on 1 and 451 DF, p-value: 0.00012

7.3 Non-parametric 2 group tests

The same conclusion is reached using a non-parametric (Wilcoxon rank sum) test.

The lm() function is part of a much more flexible modeling framework while t.test() is essentially a dead end. lm() uses of the equal variance assumption. See the companion book, *Start Modeling in R* for more details.

```
> wilcox.test(cesd ~ sex, data = HELPrct)
```

Wilcoxon rank sum test with continuity correction

```
data: cesd by sex
W = 23000, p-value = 1e-04
alternative hypothesis: true location shift is not equal to 0
```

7.4 Permutation test

Here we extend the methods introduced in section 3.6 to undertake a two-sided test comparing the ages at baseline by gender. First we calculate the observed difference in means:

```
> mean(age ~ sex, data = HELPrct)
female male
36.25 35.47
> test.stat <- diffmean(age ~ sex, data = HELPrct)
> test.stat
diffmean
-0.7841
```

We can calculate the same statistic after shuffling the group labels:

```
> do(1) * diffmean(age ~ shuffle(sex), data = HELPrct)
    diffmean
1    -0.209
> do(1) * diffmean(age ~ shuffle(sex), data = HELPrct)
    diffmean
1     0.415
> do(3) * diffmean(age ~ shuffle(sex), data = HELPrct)
    diffmean
1 -1.359219
2 -0.111150
3 -0.001026
```

```
DIGGING DEEPER
                                                                More details and examples can
> rtest.stats <- do(500) * diffmean(age ~ shuffle(sex),</pre>
                                                                be found in the mosaic package
   data = HELPrct)
                                                                Resampling Vignette.
> rtest.stats <- mutate(rtest.stats,</pre>
                        diffmeantest =
                           ifelse(diffmean >= test.stat, TRUE, FALSE))
> head(rtest.stats, 3)
  diffmean diffmeantest
1
   -0.6251
                    TRUE
2
  -1.3225
                   FALSE
3
    0.4028
                    TRUE
> favstats(~ diffmean, data = rtest.stats)
    min
              01 median
                              Q3
                                   max
                                            mean
                                                      sd
                                                           n missing
 -3.305 -0.6495 0.01121 0.6108 2.507 -0.01838 0.8981 500
                                                                    0
> gf_histogram(~ diffmean, n = 40, xlim = c(-6, 6),
   fill = ~ diffmeantest, pch = 16, cex = .8,
   data = rtest.stats) %>%
   gf_vline(xintercept = ~ test.stat, color = "red", lwd = 3)
     40 -
                                            diffmeantest
   count
                                                FALSE
                                                TRUE
     20
      0
                          0
                 -2
                                    ż
```

Here we don't see much evidence to contradict the null hypothesis that men and women have the same mean age in the population.

diffmean

7.5 One-way ANOVA

Earlier comparisons were between two groups. We can also consider testing differences between three or more groups using one-way ANOVA. Here we compare CESD scores by primary substance of abuse (heroin, cocaine, or alcohol) with a line rather a dot to indicate the median.

```
> mean(cesd ~ substance, data = HELPrct)
alcohol cocaine heroin
34.37 29.42 34.87
```

```
> anovamod <- aov(cesd ~ substance, data = HELPrct)
> summary(anovamod)
```

	Df	Sum	Sq	Mean	Sq	F	value	Pr(>F)
substance	2	27	704	13	352		8.94	0.00016
Residuals	450	686	984		L51			

While still high (scores of 16 or more are generally considered to be "severe" symptoms), the cocaine-involved group tend to have lower scores than those whose primary substances are alcohol or heroin.

> modintercept <- lm(cesd ~ 1, data = HELPrct)
> modsubstance <- lm(cesd ~ substance, data = HELPrct)</pre>

The anova() command can summarize models.

In this setting the results are identical (since there is only one predictor, with 2 df).

The anova() function can also be used to formally compare two (nested) models.

```
> anova(modintercept, modsubstance)
Analysis of Variance Table
Model 1: cesd ~ 1
Model 2: cesd ~ substance
   Res.Df RSS Df Sum of Sq F Pr(>F)
1 452 70788
2 450 68084 2 2704 8.94 0.00016
```

7.6 Tukey's Honest Significant Differences

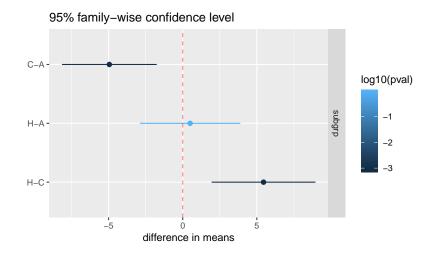
There are a variety of multiple comparison procedures that can be used after fitting an ANOVA model. One of these is Tukey's Honest Significant Differences (HSD). Other options are available within the multcomp package.

```
> favstats(cesd ~ substance, data = HELPrct)
  substance min Q1 median Q3 max mean
                                          sd
                                               n missing
1
  alcohol 4 26 36 42 58 34.37 12.05 177
                                                       0
    cocaine 1 19 30 39 60 29.42 13.40 152
2
                                                       0
3
    heroin 4 28 35 43 56 34.87 11.20 124
                                                       0
> HELPrct <- mutate(HELPrct, subgrp = factor(substance,</pre>
   levels = c("alcohol", "cocaine", "heroin"),
   labels = c("A", "C", "H")))
> mod <- lm(cesd ~ subgrp, data = HELPrct)</pre>
> HELPHSD <- TukeyHSD(mod, "subgrp")</pre>
> HELPHSD
  Tukey multiple comparisons of means
    95% family-wise confidence level
Fit: aov(formula = x)
```

\$subgrp

	diff	lwr	upr	p adj
C - A	-4.9518	-8.150	-1.753	0.0009
H-A	0.4981	-2.889	3.885	0.9362
H-C	5.4499	1.950	8.950	0.0008

> mplot(HELPHSD)



Again, we see that the cocaine group has significantly lower CESD scores than either of the other two groups.

Categorical Response, Quantitative Predictor

8.1 Logistic regression

8

Logistic regression is available using the glm() function, which supports a variety of link functions and distributional forms for generalized linear models, including logistic regression.

> logitmod <- glm(homeless ~ age + female, family = binomial, data = HELPrct) > msummary(logitmod) Coefficients: Estimate Std. Error z value Pr(>|z|)0.4537 1.97 (Intercept) 0.8926 0.049 -0.0239 0.0124 -1.92 0.055 age female 0.4920 0.2282 2.16 0.031 (Dispersion parameter for binomial family taken to be 1) Null deviance: 625.28 on 452 degrees of freedom Residual deviance: 617.19 on 450 degrees of freedom AIC: 623.2 Number of Fisher Scoring iterations: 4 > exp(coef(logitmod)) (Intercept) female age 2.4415 0.9764 1.6355 > exp(confint(logitmod)) Waiting for profiling to be done...

The glm() function has argument family, which can take an option link. The logit link is the default link for the binomial family, so we don't need to specify it here. The more verbose usage would be family=binomial(link=logit).

2.5 %	97.5 %
1.0081	5.988
0.9527	1.000
1.0501	2.574
	1.0081 0.9527

We can compare two models (for multiple degree of freedom tests). For example, we might be interested in the association of homeless status and age for each of the three substance groups.

```
> mymodsubage <- glm((homeless == "homeless") ~ age + substance,</pre>
  family = binomial, data = HELPrct)
> mymodage <- glm((homeless == "homeless") ~ age, family = binomial,</pre>
  data = HELPrct)
> msummary(mymodsubage)
Coefficients:
                Estimate Std. Error z value Pr(>|z|)
(Intercept)
                 -0.0509
                             0.5164 -0.10
                                              0.9215
                  0.0100
                             0.0129
                                       0.77
                                              0.4399
age
substancecocaine -0.7496
                             0.2303 -3.25 0.0011
substanceheroin -0.7780
                             0.2469 -3.15 0.0016
(Dispersion parameter for binomial family taken to be 1)
   Null deviance: 625.28 on 452 degrees of freedom
Residual deviance: 607.62 on 449 degrees of freedom
AIC: 615.6
Number of Fisher Scoring iterations: 4
> exp(coef(mymodsubage))
     (Intercept)
                             age substancecocaine substanceheroin
         0.9504
                          1.0101
                                           0.4725
                                                            0.4593
> anova(mymodage, mymodsubage, test = "Chisq")
Analysis of Deviance Table
Model 1: (homeless == "homeless") ~ age
Model 2: (homeless == "homeless") ~ age + substance
 Resid. Df Resid. Dev Df Deviance Pr(>Chi)
1
       451
                  622
       449
                  608 2
                            14.3 0.00078
2
```

We observe that the cocaine and heroin groups are significantly less likely to be homeless than alcohol involved subjects, after controlling for age. (A similar result is seen when considering just homeless status and substance.)

```
> tally(~ homeless | substance, format = "percent",
            margins = TRUE, data = HELPrct)
            substance
homeless alcohol cocaine heroin
            homeless 58.19 38.82 37.90
            housed 41.81 61.18 62.10
            Total 100.00 100.00
```

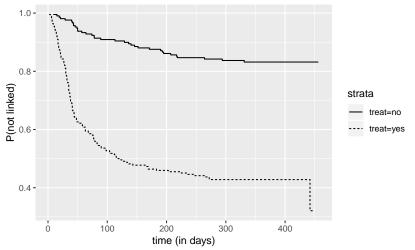
9 Survival Time Outcomes

Extensive support for survival (time to event) analysis is available within the survival package.

9.1 Kaplan-Meier plot

> library(survival)
> library(broom)
> fit <- survfit(Surv(dayslink, linkstatus) ~ treat,
 data = HELPrct)
> fit <- broom::tidy(fit)
> gf_step(fit, estimate ~ time, linetype = ~ strata,
 title = "Product-Limit Survival Estimates (time to linkage)",
 xlab = "time (in days)", ylab = "P(not linked)")

Product-Limit Survival Estimates (time to linkage)



We see that the subjects in the treatment (Health Evaluation and Linkage to Primary Care clinic) were significantly more likely to link to primary care (less likely to "survive") than the control (usual care) group.

9.2 Cox proportional hazards model

```
> library(survival)
> summary(coxph(Surv(dayslink, linkstatus) ~ age + substance,
   data = HELPrct))
Call:
coxph(formula = Surv(dayslink, linkstatus) ~ age + substance,
   data = HELPrct)
 n= 431, number of events= 163
   (22 observations deleted due to missingness)
                    coef exp(coef) se(coef)
                                               z Pr(>|z|)
                 0.00893
                           1.00897 0.01026 0.87
                                                     0.38
age
substancecocaine 0.18045
                           1.19775 0.18100 1.00
                                                     0.32
substanceheroin -0.28970
                           0.74849 0.21725 -1.33
                                                     0.18
                exp(coef) exp(-coef) lower .95 upper .95
                               0.991
                                        0.989
                                                   1.03
                    1.009
age
                    1.198
                                                   1.71
                               0.835
                                        0.840
substancecocaine
                               1.336
substanceheroin
                    0.748
                                        0.489
                                                   1.15
Concordance= 0.55 (se = 0.023 )
Rsquare= 0.014 (max possible= 0.988)
Likelihood ratio test= 6.11 on 3 df,
                                       p=0.1
Wald test
                    = 5.84 on 3 df,
                                       p=0.1
Score (logrank) test = 5.91 on 3 df,
                                       p=0.1
```

Neither age nor substance group was significantly associated with linkage to primary care.

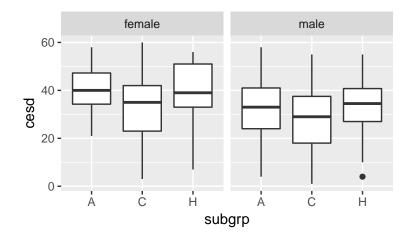
10 More than Two Variables

10.1 Two (or more) way ANOVA

We can fit a two (or more) way ANOVA model, without or with an interaction, using the same modeling syntax.

```
> HELPrct <- mutate(HELPrct, subgrp = factor(substance,
   levels = c("alcohol", "cocaine", "heroin"),
   labels = c("A", "C", "H")))
> median(cesd ~ substance | sex, data = HELPrct)
alcohol.female cocaine.female heroin.female
                                                alcohol.male
          40.0
                         35.0
                                         39.0
                                                        33.0
  cocaine.male
                  heroin.male
                                       female
                                                        male
                         34.5
                                         38.0
                                                        32.5
          29.0
```

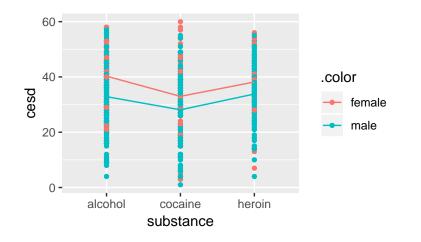
```
> gf_boxplot(cesd ~ subgrp | sex, data = HELPrct)
```



> summary(aov(cesd ~ substance + sex, data = HELPrct)) Df Sum Sq Mean Sq F value Pr(>F) substance 2 2704 1352 9.27 0.00011 1 2569 2569 17.61 3.3e-05 sex 449 146 Residuals 65515 > summary(aov(cesd ~ substance * sex, data = HELPrct)) Df Sum Sq Mean Sq F value Pr(>F) substance 2 2704 1352 9.25 0.00012 2569 2569 sex 1 17.57 3.3e-05 substance:sex 2 146 73 0.50 0.60752 65369 146 Residuals 447

There's little evidence for the interaction, though there are statistically significant main effects terms for substance group and sex.

```
> mod <- lm(cesd ~ substance + sex + substance * sex, data = HELPrct)
> plotModel(mod)
```



10.2 Multiple regression

Multiple regression is a logical extension of the prior commands, where additional predictors are added. This allows students to start to try to disentangle multivariate relationships. We tend to introduce multiple linear regression early in our courses, as a purely descriptive technique, then return to it regularly. The motivation for this is described at length in the companion volume *Start Modeling with R*. Here we consider a model (parallel slopes) for depressive symptoms as a function of Mental Component Score (MCS), age (in years) and sex of the subject.

```
> lmnointeract <- lm(cesd ~ mcs + age + sex, data = HELPrct)</pre>
> msummary(lmnointeract)
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 53.8303
                        2.3617
                                  22.79
                                          <2e-16
            -0.6548
                         0.0336 -19.50
mcs
                                          <2e-16
             0.0553
                         0.0556
                                   1.00
                                          0.3200
age
sexmale
             -2.8993
                         1.0137
                                  -2.86
                                          0.0044
Residual standard error: 9.09 on 449 degrees of freedom
Multiple R-squared: 0.476, Adjusted R-squared: 0.473
F-statistic: 136 on 3 and 449 DF, p-value: <2e-16
We can also fit a model that includes an interaction be-
tween MCS and sex.
> lminteract <- lm(cesd ~ mcs + age + sex + mcs:sex, data = HELPrct)</pre>
> msummary(lminteract)
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 55.3906
                        2.9903
                                  18.52
                                          <2e-16
            -0.7082
                        0.0712 -9.95
                                          <2e-16
mcs
             0.0549
                        0.0556 0.99
                                           0.324
age
sexmale
             -4.9421
                        2.6055 -1.90
                                           0.058
                         0.0807
                                  0.85
                                           0.395
mcs:sexmale
             0.0687
Residual standard error: 9.09 on 448 degrees of freedom
Multiple R-squared: 0.477, Adjusted R-squared: 0.472
F-statistic: 102 on 4 and 448 DF, p-value: <2e-16
> anova(lminteract)
Analysis of Variance Table
Response: cesd
           Df Sum Sq Mean Sq F value Pr(>F)
            1 32918
                       32918 398.27 <2e-16
mcs
                 107
                         107
                                1.29 0.2563
age
            1
                 676
sex
            1
                         676
                                8.18 0.0044
mcs:sex
            1
                  60
                          60
                                0.72 0.3952
Residuals 448 37028
                          83
```

> anova(lmnointeract, lminteract)
Analysis of Variance Table
Model 1: cesd ~ mcs + age + sex
Model 2: cesd ~ mcs + age + sex + mcs:sex
Res.Df RSS Df Sum of Sq F Pr(>F)
1 449 37088
2 448 37028 1 59.9 0.72 0.4

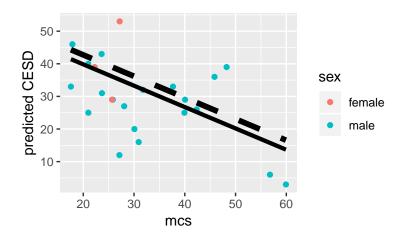
There is little evidence for an interaction effect, so we drop this from the model.

10.2.1 Visualizing the results from the regression

The makeFun() and plotFun() functions from the mosaic package can be used to display the predicted values from a regression model. For this example, we might display the predicted CESD values for a range of MCS (mental component score) values a hypothetical 36 year old male and female subject might have from the parallel slopes (no interaction) model.

> lmfunction <- makeFun(lmnointeract)</pre>

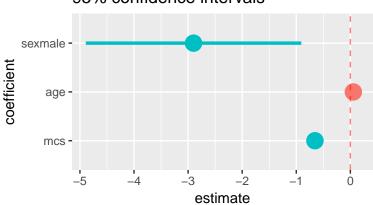
We can now plot the predicted values separately for male and female subjects over a range of MCS (mental component score) values, along with the observed data for all of the 36 year olds.



10.2.2 Coefficient plots

It is sometimes useful to display a plot of the coefficients for a multiple regression model (along with their associated confidence intervals).

> mplot(lmnointeract, rows = -1, which = 7)



Darker dots indicate regression coefficients where the 95% confidence interval does not include the null hypothesis value of zero.

CAUTION! Be careful when fitting regression models with missing values (see also section 13.11).

The mplot() function can also be used to create these graphs.

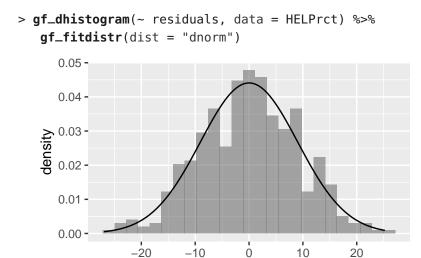
Here we are adding two new variables into an existing dataset. It's often a good practice to give the resulting dataframe a new name.

95% confidence intervals

10.2.3 Residual diagnostics

It's straightforward to undertake residual diagnostics for this model. We begin by adding the fitted values and residuals to the dataset.

```
> HELPrct <- mutate(HELPrct,
    residuals = resid(lmnointeract),
    pred = fitted(lmnointeract))
```

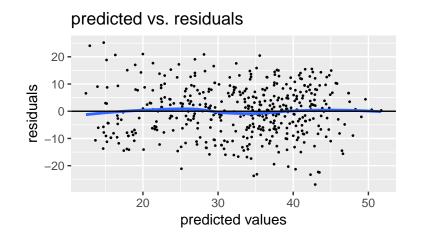


We can identify the subset of observations with extremely large residuals.

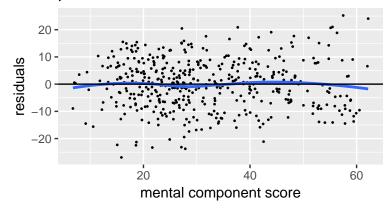
residuals

```
> filter(HELPrct, abs(residuals) > 25)
```

```
age anysubstatus anysub cesd d1 daysanysub dayslink drugrisk e2b
1 43
                 0
                       no
                             16 15
                                          191
                                                   414
                                                               0
                                                                  NA
2 27
                NA
                     <NA>
                             40 1
                                           NA
                                                               3
                                                                   2
                                                   365
  female sex glb homeless i1 i2 id indtot linkstatus link
                                                                mcs
       0 male no homeless 24 36 44
1
                                          41
                                                      0
                                                           no 15.86
2
       0 male no homeless 18 18 420
                                          37
                                                      0
                                                           no 57.49
    pcs pss_fr racegrp satreat sexrisk substance treat avg_drinks
1 71.39
                 white
                                      7
                                          cocaine
             3
                            no
                                                    yes
                                                                 24
2 37.75
                                      3
                                           heroin
                                                                 18
             8
                 white
                           yes
                                                     no
 max_drinks subgrp residuals pred
          36
                       -26.92 42.92
1
                  С
2
          18
                        25.22 14.78
                  Н
```



predicted vs. residuals



The assumptions of normality, linearity and homoscedasticity seem reasonable here.

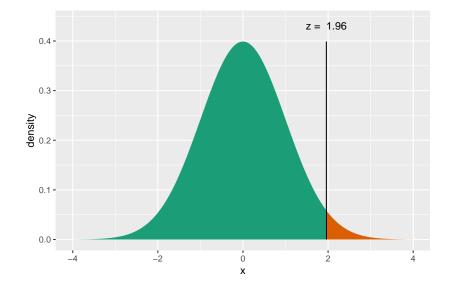
11 Probability Distributions & Random Variables

R can calculate quantities related to probability distributions of all types. It is straightforward to generate random samples from these distributions, which can be used for simulation and exploration.

> xpnorm(1.96, mean = 0, sd = 1) # P(Z < 1.96)</pre>

If X ~ N(0, 1), then P(X <= 1.96) = P(Z <= 1.96) = 0.975 P(X > 1.96) = P(Z > 1.96) = 0.025

[1] 0.975

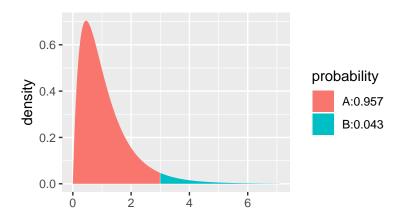


> # value which satisfies P(Z < z) = 0.975
> qnorm(.975, mean = 0, sd = 1)
[1] 1.96
> integrate(dnorm, -Inf, 0) # P(Z < 0)
0.5 with absolute error < 4.7e-05</pre>

A similar display is available for the F distribution.

```
> xpf(3, df1 = 4, df2 = 20)
```

[1] 0.9568



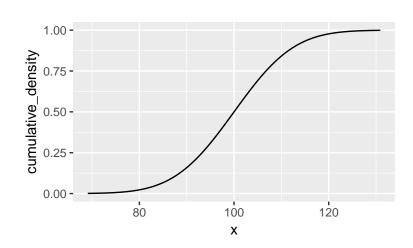
The following table displays the basenames for probability distributions available within base R. These functions can be prefixed by d to find the density function for the distribution, p to find the cumulative distribution function, q to find quantiles, and r to generate random draws. For example, to find the density function of an exponential random variable, use the command dexp(). The qDIST() function is the inverse of the pDIST() function, for a given basename DIST.

Distribution	Basename
Beta	beta
binomial	binom
Cauchy	cauchy
chi-square	chisq
exponential	exp
F	f
gamma	gamma
geometric	geom
hypergeometric	hyper
logistic	logis
lognormal	lnorm
negative binomial	nbinom
normal	norm
Poisson	pois
Student's t	t
Uniform	unif
Weibull	weibull

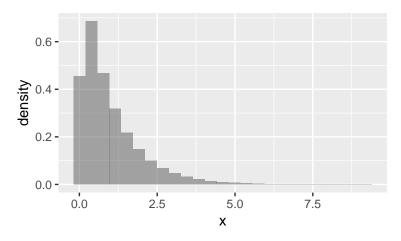
The gf_dist() can be used to display distributions in a variety of ways.

DIGGING DEEPER The gf_fitdistr() facilitates estimation of parameters for many distributions.

> gf_dist('norm', mean = 100, sd = 10, kind = 'cdf')



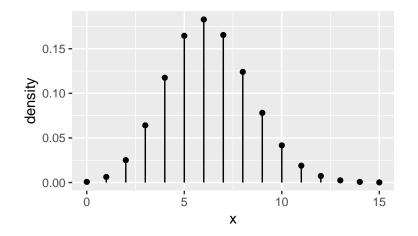
> gf_dist('exp', kind = 'histogram', xlab = "x")



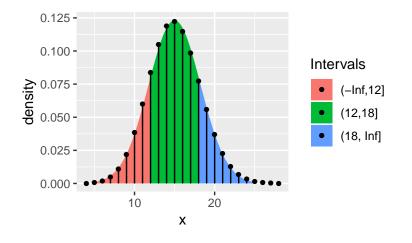
Note that this sets the rate parameter to 1 by default and is equivalent to the following command.

> gf_dist('exp', rate = 1, kind = 'histogram', xlab = "x")

> gf_dist('binom', size = 25, prob = 0.25, xlim = c(-1, 26))



Multiple distributions can be plotted on the same plot.



The gf_fun() function can be used to plot an arbitrary function (in this case an exponential random variable).

```
> f <- makeFun(2 * exp(-2 * x) ~ x) # exponential with rate parameter 2
> x <- rexp(1000, rate = 2)
> gf_dhistogram(~ x, binwidth = 0.2, center = 0.1) %>%
gf_fun(f(x) ~ x, color = "red", size = 2, xlim = c(0, 3))
2.0-
1.5-
1.0-
0.5-
0.0-
0.1 1 2 3
x
```

12 Power Calculations

While not generally a major topic in introductory courses, power and sample size calculations help to reinforce key ideas in statistics. In this section, we will explore how R can be used to undertake power calculations using analytic approaches. We consider a simple problem with two tests (t-test and sign test) of a one-sided comparison.

We will compare the power of the sign test and the power of the test based on normal theory (one sample one sided t-test) assuming that σ is known. Let $X_1, ..., X_{25}$ be i.i.d. N(0.3, 1) (this is the alternate that we wish to calculate power for). Consider testing the null hypothesis $H_0: \mu = 0$ versus $H_A: \mu > 0$ at significance level $\alpha = .05$.

12.1 Sign test

We start by calculating the Type I error rate for the sign test. Here we want to reject when the number of positive values is large. Under the null hypothesis, this is distributed as a Binomial random variable with n=25 trials and p=0.5 probability of being a positive value. Let's consider values between 15 and 19.

> qbinom(.95, size = 25, prob = 0.5)
[1] 17

So we see that if we decide to reject when the number of positive values is 17 or larger, we will have an α level of 0.054, which is near the nominal value in the problem.

We calculate the power of the sign test as follows. The probability that $X_i > 0$, given that H_A is true is given by:

```
> 1 - pnorm(0, mean = 0.3, sd = 1)
```

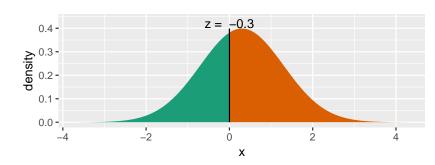
```
[1] 0.6179
```

[1] 0.6179

We can view this graphically using the command:

> xpnorm(0, mean = 0.3, sd = 1, lower.tail = FALSE)

If $X \sim N(0.3, 1)$, then $P(X \le 0) = P(Z \le -0.3) = 0.3821$ P(X > 0) = P(Z > -0.3) = 0.6179



The power under the alternative is equal to the probability of getting 17 or more positive values, given that p = 0.6179:

```
> 1 - pbinom(16, size = 25, prob = 0.6179)
[1] 0.3378
```

The power is modest at best.

12.2 *T-test*

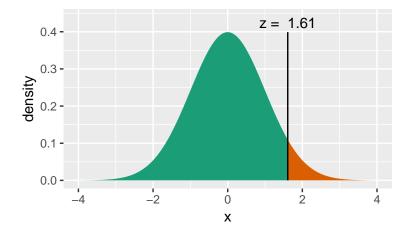
We next calculate the power of the test based on normal theory. To keep the comparison fair, we will set our α level equal to 0.05388.

```
> alpha <- 1 - pbinom(16, size = 25, prob = 0.5)
> alpha
[1] 0.05388
```

First we find the rejection region.

```
> n <- 25
> sigma <- 1 # given
> stderr <- sigma/sqrt(n)
> zstar <- xqnorm(1 - alpha, mean = 0, sd = 1)
If X ~ N(0, 1), then
P(X <= 1.608) = 0.9461
P(X > 1.608) = 0.05388
> zstar
[1] 1.608
> crit <- zstar * stderr
> crit
```

[1] 0.3217



Therefore, we reject for observed means greater than 0.322.

To calculate the power of this one-sided test we find the probability under the alternative hypothesis to the right of this cutoff.

```
> power <- 1 - pnorm(crit, mean = 0.3, sd = stderr)
> power
[1] 0.4568
```

The power of the test based on normal theory is 0.457. To provide a check (or for future calculations of this sort) we can use the power.t.test() function.

[1] 0.4408

This analytic (formula-based approach) yields a similar estimate to the value that we calculated directly.

Overall, we see that the t-test has higher power than the sign test, if the underlying data are truly normal.

Calculating power empirically demonstrates the power of simulations.

13 Data Wrangling

Data wrangling (also known as management, curation, or marshaling) is a key capacity to allow students (and instructors) to "compute with data" or as Diane Lambert of Google has stated, "think with data". We tend to keep student data wrangling to a minimum during the early part of an introductory statistics course, then gradually introduce topics as needed. For courses where students undertake substantive projects, more focus on data management is needed. This chapter describes some key data management tasks.

Inspecting dataframes 13.1

1

0

The inspect() function can be helpful in describing the variables in a dataframe (the name for a dataset in R).

```
> inspect(iris)
categorical variables:
     name class levels
                          n missing
1 Species factor
                      3 150
                                  0
                                   distribution
1 setosa (33.3%), versicolor (33.3%) ...
quantitative variables:
          name
                 class min Q1 median Q3 max mean
1 Sepal.Length numeric 4.3 5.1
                                 5.80 6.4 7.9 5.843 0.8281 150
2
  Sepal.Width numeric 2.0 2.8
                                 3.00 3.3 4.4 3.057 0.4359 150
3 Petal.Length numeric 1.0 1.6
                                 4.35 5.1 6.9 3.758 1.7653 150
  Petal.Width numeric 0.1 0.3
                                 1.30 1.8 2.5 1.199 0.7622 150
4
 missina
```

```
The Start Teaching with R book
features an extensive section on
data management, including
use of the read.file() function
to load data into R and RStudio.
```

The dplyr and tidyr packages provide an elegant approach to data management and facilitate the ability of students to compute with data. Hadley Wickham, author of the packages, suggests that there are six key idioms (or verbs) implemented within these packages that allow a large set of tasks to be accomplished: filter (keep rows matching criteria), select (pick columns by name), arrange (reorder rows), mutate (add new variables), summarise (reduce variables to values), and group by (collapse groups). See https://nhorton.people. amherst.edu/precursors for more details and resources.

sd

2 0 3 0 4 0

The iris dataframe includes one categorical and four quantitative variables.

13.2 Adding new variables to a dataframe

We can add additional variables to an existing dataframe using mutate(). But first we create a smaller version of the iris dataframe.

```
> irisSmall <- select(iris, Species, Sepal.Length)
> # cut places data into bins
```

```
> irisSmall <- mutate(irisSmall,
    Length = cut(Sepal.Length, breaks = 4:8))
```

Multiple commands can be chained together using the %>% (pipe) operator:

```
> irisSmall <- iris %>%
select(Species, Sepal.Length) %>%
mutate(Length = cut(Sepal.Length, breaks = 4:8))
```

Note that in this usage the first argument to select() is the first variable (as it inherits the data from the previous pipe).

```
> head(irisSmall)
Species Sepal.Length Length
1 setosa 5.1 (5,6]
2 setosa 4.9 (4,5]
3 setosa 4.7 (4,5]
4 setosa 4.6 (4,5]
5 setosa 5.0 (4,5]
6 setosa 5.4 (5,6]
```

The cut() function has an option labels which can be used to specify more descriptive names for the groups. The CPS85 dataframe contains data from a Current Population Survey (current in 1985, that is). Two of the variables in this dataframe are age and educ. We can estimate the number of years a worker has been in the workforce if we assume they have been in the workforce since completing their education and that their age at graduation is 6 more than the number of years of education obtained. We can add this as a new variable in the dataframe using mutate().

```
> CPS85 <- mutate(CPS85, workforce.years = age - 6 - educ)
> favstats(~ workforce.years, data = CPS85)
min Q1 median Q3 max mean sd n missing
-4 8 15 26 55 17.81 12.39 534 0
```

In fact this is what was done for all but one of the cases to create the exper variable that is already in the CPS85 data.

```
> tally(~ (exper - workforce.years), data = CPS85)
  (exper - workforce.years)
    0    4
533    1
```

13.3 Dropping variables

Since we already have the exper variable, there is no reason to keep our new variable. Let's drop it. Notice the clever use of the minus sign.

```
> names(CPS85)
 [1] "wage"
                        "educ"
                                           "race"
 [4] "sex"
                        "hispanic"
                                           "south"
 [7] "married"
                        "exper"
                                           "union"
[10] "age"
                        "sector"
                                           "workforce.years"
> CPS1 <- select(CPS85, select = -matches("workforce.years"))</pre>
> names(CPS1)
 [1] "wage"
                 "educ"
                            "race"
                                        "sex"
                                                    "hispanic" "south"
 [7] "married" "exper"
                                        "age"
                                                    "sector"
                            "union"
```

Any number of variables can be dropped or kept in a similar manner.

> CPS1 <- select(CPS85, select = -matches("workforce.years|exper"))</pre>

13.4 Renaming variables

The column (variable) names for a dataframe can be changed using the rename() function in the dplyr package.

```
> names(CPS85)
 [1] "wage"
                       "educ"
                                         "race"
 [4] "sex"
                       "hispanic"
                                         "south"
[7] "married"
                       "exper"
                                         "union"
                                         "workforce.years"
[10] "age"
                       "sector"
> CPSnew <- rename(CPS85, workforce = workforce.years)</p>
> names(CPSnew)
[1] "wage"
                 "educ"
                             "race"
                                         "sex"
                                                     "hispanic"
[6] "south"
                "married"
                             "exper"
                                         "union"
                                                     "age"
```

[11] "sector" "workforce"

The row names of a dataframes can be changed by simple assignment using row.names().

The faithful data set (in the datasets package, which is always available) has very unfortunate names.

```
> names(faithful)
```

[1] "eruptions" "waiting"

It's a good idea to establish practices for choice of variable names from day one.

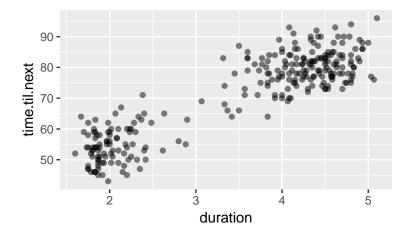
The measurements are the duration of an eruption and the time until the subsequent eruption, so let's give it some better names.

```
> faithful <- rename(faithful,
    duration = eruptions, # new = old
    time.til.next = waiting)
```

```
> names(faithful)
```

[1] "duration" "time.til.next"

> gf_point(time.til.next ~ duration, alpha = 0.5, data = faithful)



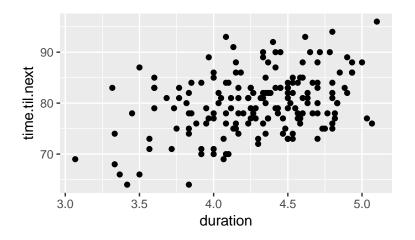
If the variable containing a dataframe is modified or used to store a different object, the original data from the package can be recovered using data().

13.5 Creating subsets of observations

We can also use filter() to reduce the size of a dataframe by selecting only certain rows.

```
> data(faithful)
> names(faithful) <- c('duration', 'time.til.next')</pre>
```

```
> # any logical can be used to create subsets
> faithfulLong <- filter(faithful, duration > 3)
> gf_point(time.til.next ~ duration, data = faithfulLong)
```



13.6 Sorting dataframes

Data frames can be sorted using the arrange() function.

```
> head(faithful, 3)
  duration time.til.next
1
     3.600
                        79
2
     1.800
                        54
3
     3.333
                        74
> sorted <- arrange(faithful, duration)</pre>
> head(sorted, 3)
  duration time.til.next
     1.600
                        52
1
                        64
2
     1.667
3
     1.700
                        59
```

CAUTION! It is usually better to make new datasets rather than modifying the original.

13.7 Merging datasets

The fusion1 dataframe in the fastR package contains genotype information for a SNP (single nucleotide poly-

morphism) in the gene *TCF7L2*. The pheno dataframe contains phenotypes (including type 2 diabetes case/control status) for an intersecting set of individuals. We can join (or merge) these together to explore the association between genotypes and phenotypes using merge().

```
> library(fastR)
> fusion1 <- arrange(fusion1, id)</pre>
> head(fusion1, 3)
           marker markerID allele1 allele2 genotype Adose Cdose Gdose Tdose
    id
1 1002 RS12255372
                          1
                                  3
                                          3
                                                   GG
                                                          0
                                                                0
                                                                       2
                                                                             0
                                                                       2
2 1009 RS12255372
                          1
                                  3
                                          3
                                                   GG
                                                          0
                                                                0
                                                                             0
3 1012 RS12255372
                          1
                                  3
                                          3
                                                   GG
                                                          0
                                                                0
                                                                       2
                                                                             0
> head(pheno, 3)
                            age smoker chol waist weight height
    id
           t2d
                 bmi sex
                                                                    whr sbp dbp
1 1002
          case 32.86
                        F 70.76 former 4.57 112.0
                                                     85.6 161.4 0.9868 135
                                                                              77
2 1009
          case 27.39
                        F 53.92 never 7.32 93.5
                                                     77.4 168.1 0.9397 158
                                                                              88
3 1012 control 30.47
                       M 53.86 former 5.02 104.0
                                                     94.6 176.2 0.9327 143
                                                                              89
> library(tidyr)
> fusion1m <- inner_join(fusion1, pheno, by = 'id')</pre>
> head(fusion1m, 3)
    id
           marker markerID allele1 allele2 genotype Adose Cdose Gdose Tdose
                                                                                   t2d
                                                                                          bmi
1 1002 RS12255372
                                  3
                                          3
                                                          0
                                                                0
                                                                       2
                                                                             0
                                                                                  case 32.86
                          1
                                                   GG
                                  3
                                          3
                                                                       2
2 1009 RS12255372
                          1
                                                   GG
                                                          0
                                                                0
                                                                             0
                                                                                  case 27.39
                                                                       2
3 1012 RS12255372
                          1
                                  3
                                          3
                                                   GG
                                                          0
                                                                0
                                                                             0 control 30.47
  sex
        age smoker chol waist weight height
                                                whr sbp dbp
1
    F 70.76 former 4.57 112.0
                                 85.6 161.4 0.9868 135
                                                          77
2
    F 53.92 never 7.32 93.5
                                 77.4 168.1 0.9397 158
                                                          88
    M 53.86 former 5.02 104.0
3
                                 94.6 176.2 0.9327 143
                                                          89
```

Now we are ready to begin our analysis.

> tally(~ t2d + genotype, data = fusion1m)

genotype			
t2d	GG	GT	ΤT
case	737	375	48
control	835	309	27

13.8 Slicing and dicing

The tidyr package provides a flexible way to change the arrangement of data. It was designed for converting between long and wide versions of time series data and its arguments are named with that in mind.

A common situation is when we want to convert from a wide form to a long form because of a change in perspective about what a unit of observation is. For example, in the traffic dataframe, each row is a year, and data for multiple states are provided. The vignettes that accompany the tidyr and dplyr packages feature a number of useful examples of common data manipulations.

> traffic

	year	cn.deaths	ny	cn	ma	ri
1	1951	265	13.9	13.0	10.2	8.0
2	1952	230	13.8	10.8	10.0	8.5
3	1953	275	14.4	12.8	11.0	8.5
4	1954	240	13.0	10.8	10.5	7.5
5	1955	325	13.5	14.0	11.8	10.0
6	1956	280	13.4	12.1	11.0	8.2
7	1957	273	13.3	11.9	10.2	9.4
8	1958	248	13.0	10.1	11.8	8.6
9	1959	245	12.9	10.0	11.0	9.0

We can reformat this so that each row contains a measurement for a single state in one year.

```
> longTraffic <- traffic %>%
   gather(state, deathRate, ny:ri)
> head(longTraffic)
  year cn.deaths state deathRate
1 1951
             265
                     ny
                             13.9
2 1952
             230
                             13.8
                     ny
3 1953
             275
                             14.4
                     ny
4 1954
             240
                             13.0
                     ny
5 1955
             325
                             13.5
                     ny
6 1956
             280
                     ny
                             13.4
```

We can also reformat the other way, this time having all data for a given state form a row in the dataframe.

```
> stateTraffic <- longTraffic %>%
   select(year, deathRate, state) %>%
   mutate(year = paste("deathRate.", year, sep = "")) %>%
   spread(year, deathRate)
> stateTraffic
  state deathRate.1951 deathRate.1952 deathRate.1953 deathRate.1954 deathRate.1955
                                                 12.8
1
                  13.0
                                  10.8
                                                                 10.8
                                                                                14.0
     cn
2
                  10.2
                                  10.0
                                                 11.0
                                                                 10.5
                                                                                11.8
     ma
3
                  13.9
                                  13.8
                                                 14.4
                                                                 13.0
                                                                                13.5
     ny
                   8.0
                                   8.5
                                                  8.5
                                                                 7.5
                                                                                10.0
4
     ri
  deathRate.1956 deathRate.1957 deathRate.1958 deathRate.1959
            12.1
                           11.9
                                           10.1
                                                          10.0
1
2
            11.0
                           10.2
                                           11.8
                                                          11.0
3
            13.4
                           13.3
                                           13.0
                                                          12.9
4
             8.2
                            9.4
                                            8.6
                                                           9.0
```

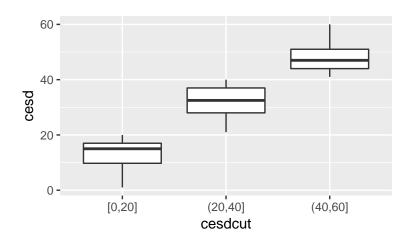
13.9 Derived variable creation

A number of functions help facilitate the creation or recoding of variables.

13.9.1 Creating categorical variable from a quantitative variable

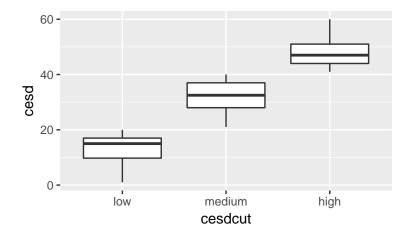
Next we demonstrate how to create a three-level categorical variable with cuts at 20 and 40 for the CESD scale (which ranges from 0 to 60 points).

```
> favstats(~ cesd, data = HELPrct)
min Q1 median Q3 max mean sd n missing
1 25 34 41 60 32.85 12.51 453 0
> HELPrct <- mutate(HELPrct, cesdcut = cut(cesd,
            breaks = c(0, 20, 40, 60), include.lowest = TRUE))
> gf_boxplot(cesd ~ cesdcut, data = HELPrct)
```



It might be preferable to give better labels.

```
> HELPrct <- mutate(HELPrct, cesdcut = cut(cesd,
    labels = c("low", "medium", "high"),
    breaks = c(0, 20, 40, 60), include.lowest = TRUE))
> gf_boxplot(cesd ~ cesdcut, data = HELPrct)
```



The case_when() function is even more general and can also be used for this purpose.

```
> HELPrct <- mutate(HELPrct,
anothercut = case_when(
    cesd >= 0 & cesd <= 20 ~ "low",
    cesd > 20 & cesd <= 40 ~ "medium",
    cesd > 40 ~ "high"))
```

The ntiles() function can be used to automate creation of groups in this manner.

13.9.2 *Reordering factors*

By default R uses the first level in lexicographic order as the reference group for modeling. This can be overriden using the relevel() function (see also reorder()).

```
> tally(~ substance, data = HELPrct)
substance
alcohol cocaine heroin
    177
           152
                    124
> coef(lm(cesd ~ substance, data = HELPrct))
     (Intercept) substancecocaine substanceheroin
         34.3729
                        -4.9518
                                            0.4981
> HELPrct <- mutate(HELPrct, subnew = relevel(substance,</pre>
   ref = "heroin"))
> coef(lm(cesd ~ subnew, data = HELPrct))
  (Intercept) subnewalcohol subnewcocaine
      34.8710
                  -0.4981
                              -5.4499
```

13.10 Group-wise statistics

It can often be useful to calculate summary statistics by group, and add these into a dataset. The group_by() function in the dplyr package facilitates this process. Here we demonstrate how to add a variable containing the median age of subjects by substance group.

```
> favstats(age ~ substance, data = HELPrct)
  substance min Q1 median
                            Q3 max mean
                                                 n missing
                                            sd
1
   alcohol 20 33
                    38.0 43.00 58 38.20 7.652 177
                                                         0
2
    cocaine 23 30
                    33.5 37.25 60 34.49 6.693 152
                                                         0
3
    heroin 19 27 33.0 39.00 55 33.44 7.986 124
                                                         0
> ageGroup <- HELPrct %>%
  group_by(substance) %>%
  summarise(agebygroup = mean(age))
> ageGroup
```

```
# A tibble: 3 x 2
  substance agebygroup
  <fct>
                 <dbl>
1 alcohol
                  38.2
2 cocaine
                  34.5
3 heroin
                  33.4
> nrow(ageGroup)
[1] 3
> nrow(HELPrct)
[1] 453
> HELPmerged <- left_join(ageGroup, HELPrct, by = "substance")</pre>
> favstats(agebygroup ~ substance, data = HELPmerged)
                     01 median
  substance
              min
                                   Q3
                                                        n missing
                                        max mean sd
1
    alcohol 38.20 38.20 38.20 38.20 38.20 38.20 0 177
                                                                0
2
    cocaine 34.49 34.49 34.49 34.49 34.49 34.49 0 152
                                                                0
     heroin 33.44 33.44 33.44 33.44 33.44 33.44 0 124
3
                                                                0
> nrow(HELPmerged)
[1] 453
```

13.11 Accounting for missing data

Missing values arise in almost all real world investigations. R uses the NA character as an indicator for missing data. The HELPmiss dataframe within the mosaicData package includes all n = 470 subjects enrolled at baseline (including the n = 17 subjects with some missing data who were not included in HELPrct).

```
> smaller <- select(HELPmiss, cesd, drugrisk, indtot, mcs, pcs,
    substance)
> dim(smaller)
[1] 470 6
> summary(smaller)
    cesd drugrisk indtot mcs
```

pcs

Min. : 1.0 Min. : 0.00 Min. : 4.0 Min. : 6.76 Min. :14.1 1st Qu.:25.0 1st Qu.:32.0 1st Qu.:21.66 1st Qu.: 0.00 1st Qu.:40.4 Median :34.0 Median : 0.00 Median :37.5 Median :28.56 Median :48.9 :32.9 :35.7 Mean Mean : 1.87 Mean Mean :31.55 Mean :48.1 3rd Qu.:41.0 3rd Qu.: 1.00 3rd Qu.:41.0 3rd Qu.:40.64 3rd Qu.:57.0 :60.0 :21.00 :45.0 :74.8 Max. Max. Max. Max. :62.18 Max. NA's :2 NA's :14 NA's :2 NA's :2 substance alcohol:185 cocaine:156 heroin :128 missing: 1

Of the 470 subjects in the 6 variable dataframe, only the drugrisk, indtot, mcs, and pcs variables have missing values.

```
> favstats(~ mcs, data = smaller)
   min
          Q1 median
                        Q3
                             max mean
                                           sd
                                                n missing
 6.763 21.66 28.56 40.64 62.18 31.55 12.78 468
                                                         2
> with(smaller, sum(is.na(mcs)))
[1] 2
> nomiss <- na.omit(smaller)</pre>
> dim(nomiss)
[1] 453
          6
> nrow(nomiss)
[1] 453
> ncol(nomiss)
[1] 6
> favstats(~ mcs, data = nomiss)
          01 median
                        Q3
   min
                             max mean
                                          sd
                                               n missing
 6.763 21.79
               28.6 40.94 62.18 31.7 12.82 453
                                                        0
```

Alternatively, we could generate the same dataset using logical conditions.

```
> nomiss <- filter(smaller,
   (!is.na(mcs) & !is.na(indtot) & !is.na(drugrisk)))
> dim(nomiss)
```

[1] 453 6

14 Health Evaluation (HELP) Study

Many of the examples in this guide utilize data from the HELP study, a randomized clinical trial for adult inpatients recruited from a detoxification unit. Patients with no primary care physician were randomized to receive a multidisciplinary assessment and a brief motivational intervention or usual care, with the goal of linking them to primary medical care. Funding for the HELP study was provided by the National Institute on Alcohol Abuse and Alcoholism (Ro1-AA10870, Samet PI) and National Institute on Drug Abuse (Ro1-DA10019, Samet PI). The details of the randomized trial along with the results from a series of additional analyses have been published¹.

Eligible subjects were adults, who spoke Spanish or English, reported alcohol, heroin or cocaine as their first or second drug of choice, resided in proximity to the primary care clinic to which they would be referred or were homeless. Patients with established primary care relationships they planned to continue, significant dementia, specific plans to leave the Boston area that would prevent research participation, failure to provide contact information for tracking purposes, or pregnancy were excluded.

Subjects were interviewed at baseline during their detoxification stay and follow-up interviews were undertaken every 6 months for 2 years. A variety of continuous, count, discrete, and survival time predictors and outcomes were collected at each of these five occasions. The Institutional Review Board of Boston University Medical Center approved all aspects of the study, including the creation of the de-identified dataset. Additional privacy protection was secured by the issuance of a Certificate of Confidentiality by the Department of Health and Human

¹ J. H. Samet, M. J. Larson, N. J. Horton, K. Doyle, M. Winter, and R. Saitz. Linking alcohol and drug dependent adults to primary medical care: A randomized controlled trial of a multidisciplinary health intervention in a detoxification unit. Addiction, 98(4):509–516, 2003; J. Liebschutz, J. B. Savetsky, R. Saitz, N. J. Horton, C. Lloyd-Travaglini, and J. H. Samet. The relationship between sexual and physical abuse and substance abuse consequences. Journal of Substance Abuse Treatment, 22(3):121-128, 2002; and S. G. Kertesz, N. J. Horton, P. D. Friedmann, R. Saitz, and J. H. Samet. Slowing the revolving door: stabilization programs reduce homeless persons' substance use after detoxification. Journal of Substance Abuse Treatment, 24(3):197-207, 2003

Services.

The mosaicData package contains several forms of the de-identified HELP dataset. We will focus on HELPrct, which contains 27 variables for the 453 subjects with minimal missing data, primarily at baseline. Variables included in the HELP dataset are described in Table 14.1. More information can be found at: https://nhorton.people.amherst.edu/r2. A copy of the study instruments can be found at: https://nhorton.people.amherst.edu/ help.

Table 14.1: Annotated description of variables in the HELPrct dataset

VARIABLE	DESCRIPTION (VALUES)	NOTE
age	age at baseline (in years) (range	
	19–60)	
anysub	use of any substance post-detox	see also
		daysanysub
cesd	Center for Epidemiologic Stud-	
	ies Depression scale (range 0–60,	
	higher scores indicate more depres-	
	sive symptoms)	
dl	how many times hospitalized for	
	medical problems (lifetime) (range	
	0–100)	
daysanysub	time (in days) to first use of any	see also
	substance post-detox (range 0–268)	anysubstatus
dayslink	time (in days) to linkage to primary	see also
	care (range 0–456)	linkstatus
drugrisk	Risk-Assessment Battery (RAB)	see also sexrisk
	drug risk score (range 0–21)	
e2b	number of times in past 6 months	
	entered a detox program (range	
	1–21)	
female	gender of respondent (o=male,	
	1=female)	
glb	experienced serious thoughts of	
	suicide (last 30 days, values o=no,	
	1=yes)	
homeless	1 or more nights on the street or	
	shelter in past 6 months (o=no,	
	1=yes)	

i1	average number of drinks (standard	see also i2
	units) consumed per day (in the	
	past 30 days, range 0–142)	
i2	maximum number of drinks (stan-	see also i1
	dard units) consumed per day (in	
	the past 30 days range 0–184)	
id	random subject identifier (range	
	1–470)	
indtot	Inventory of Drug Use Conse-	
	quences (InDUC) total score (range	
	4-45)	
linkstatus	post-detox linkage to primary care	see also dayslink
	(0=no, 1=yes)	
mcs	SF-36 Mental Component Score	see also pcs
	(range 7-62, higher scores are bet-	
	ter)	
pcs	SF-36 Physical Component Score	see also mcs
	(range 14-75, higher scores are	
	better)	
pss_fr	perceived social supports (friends,	
	range 0–14)	
racegrp	race/ethnicity (black, white, his-	
	panic or other)	
satreat	any BSAS substance abuse treat-	
	ment at baseline (0=no, 1=yes)	
sex	sex of respondent (male or female)	
sexrisk	Risk-Assessment Battery (RAB) sex	see also drugrisk
	risk score (range 0–21)	
substance	primary substance of abuse (alco-	
	hol, cocaine or heroin)	
treat	randomization group (randomize to	
	HELP clinic, no or yes)	

Notes: Observed range is provided (at baseline) for continuous variables.

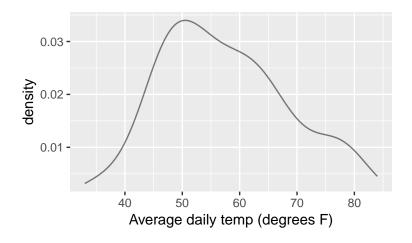
15 Exercises and Problems

The first part of the exercise number indicates which chapter it comes from.

3.1. Using the HELPrct dataset, create side-by-side histograms of the CESD scores by substance abuse group, just for the male subjects, with an overlaid normal density.

5.1. Using the HELPrct dataset, fit a simple linear regression model predicting the number of drinks per day as a function of the mental component score. This model can be specified using the formula: $i1 \sim mcs$. Assess the distribution of the residuals for this model.

10.1. The RailTrail dataset within the mosaic package includes the counts of crossings of a rail trail in Northampton, Massachusetts for 90 days in 2005. City officials are interested in understanding usage of the trail network, and how it changes as a function of temperature and day of the week. Describe the distribution of the variable avgtemp in terms of its center, spread and shape.



10.2. The RailTrail dataset also includes a variable called cloudcover. Describe the distribution of this variable in terms of its center, spread and shape.

10.3. The variable in the RailTrail dataset that provides the daily count of crossings is called volume. Describe the distribution of this variable in terms of its center, spread and shape.

10.4. The RailTrail dataset also contains an indicator of whether the day was a weekday (weekday==1) or a weekend/holiday (weekday==0). Use tally() to describe the distribution of this categorical variable. What percentage of the days are weekends/holidays?

10.5. Use side-by-side boxplots to compare the distribution of volume by day type in the RailTrail dataset. Hint: you'll need to turn the numeric weekday variable into a factor variable using as.factor() or use the horizontal=FALSE option. What do you conclude?

10.6. Use overlapping densityplots to compare the distribution of volume by day type in the RailTrail dataset. What do you conclude?

10.7. Create a scatterplot of volume as a function of avgtemp using the RailTrail dataset, along with a regression line and scatterplot smoother (lowess curve). What do you observe about the relationship?

10.8. Using the RailTrail dataset, fit a multiple regression model for volume as a function of cloudcover, avgtemp,

weekday and the interaction between day type and average temperature. Is there evidence to retain the interaction term at the $\alpha = 0.05$ level?

10.9. Use makeFun() to calculate the predicted number of crossings on a weekday with average temperature 60 degrees and no clouds. Verify this calculation using the coefficients from the model.

```
> coef(fm)
```

(Intercept)	cloudcover	avgtemp
378.834	-17.198	2.313
weekdayTRUE	avgtemp:weekdayTRUE	
-321.116	4.727	

10.10. Use makeFun() and gf_fun() to display predicted values for the number of crossings on weekdays and weekends/holidays for average temperatures between 30 and 80 degrees and a cloudy day (cloudcover=10).

10.11. Using the multiple regression model, generate a histogram (with overlaid normal density) to assess the normality of the residuals.

10.12. Using the same model generate a scatterplot of the residuals versus predicted values and comment on the linearity of the model and assumption of equal variance.

10.13. Using the same model generate a scatterplot of the residuals versus average temperature and comment on the linearity of the model and assumption of equal variance.

11.1. Generate a sample of 1000 exponential random variables with rate parameter equal to 2, and calculate the mean of those variables.

11.2. Find the median of the random variable *X*, if it is exponentially distributed with rate parameter 10.

12.1. Find the power of a two-sided two-sample t-test where both distributions are approximately normally distributed with the same standard deviation, but the group differ by 50% of the standard deviation. Assume

that there are 25 observations per group and an alpha level of 0.0539.

12.2. Find the sample size needed to have 90% power for a two group t-test where the true difference between means is 25% of the standard deviation in the groups (with $\alpha = 0.05$).

13.1. Using faithful dataframe, make a scatter plot of eruption duration times vs. the time since the previous eruption.

13.2. The fusion2 data set in the fastR package contains genotypes for another SNP. Merge fusion1, fusion2, and pheno into a single data frame.

Note that fusion1 and fusion2 have the same columns.

```
> names(fusion1)
[1] "id" "marker" "markerID" "allele1" "allele2" "genotype" "Adose"
[8] "Cdose" "Gdose" "Tdose"
> names(fusion2)
[1] "id" "marker" "markerID" "allele1" "allele2" "genotype" "Adose"
[8] "Cdose" "Gdose" "Tdose"
```

You may want to use the suffixes argument to merge() or rename the variables after you are done merging to make the resulting dataframe easier to navigate.

Tidy up your dataframe by dropping any columns that are redundant or that you just don't want to have in your final dataframe.

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